

The GAPS programme at TNG

XL. A puffy and warm Neptune-sized planet and an outer Neptune-mass candidate orbiting the solar-type star TOI-1422

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ABSTRACT

Context. Neptunes represent one of the main types of exoplanets and have chemical-physical characteristics halfway between rocky and gas giant planets. Therefore, their characterization is important for understanding and constraining both the formation mechanisms and the evolution patterns of planets.

Aims. We investigate the exoplanet candidate TOI-1422 b, which was discovered by the TESS space telescope around the high proper-motion G2 V star TOI-1422 ($V = 10.6$ mag), 155 pc away, with the primary goal of confirming its planetary nature and characterising its properties.

Methods. We monitored TOI-1422 with the HARPS-N spectrograph for 1.5 yr to precisely quantify its radial velocity (RV) variation. We analyse these RV measurements jointly with TESS photometry and check for blended companions through high-spatial resolution images using the AstraLux instrument.

Results. We estimate that the parent star has a radius of $R_{\star} = 1.019^{+0.014}_{-0.013} R_{\odot}$, and a mass of $M_{\star} = 0.981^{+0.062}_{-0.065} M_{\odot}$. Our analysis confirms the planetary nature of TOI-1422 b and also suggests the presence of a Neptune-mass planet on a more distant orbit, the candidate TOI-1422 c, which is not detected in TESS light curves. The inner planet, TOI-1422 b, orbits on a period of $P_b = 12.9972 \pm 0.0006$ days and has an equilibrium temperature of $T_{\text{eq},b} = 867 \pm 17$ K. With a radius of $R_b = 3.96^{+0.13}_{-0.11} R_{\oplus}$, a mass of $M_b = 9.0^{+2.3}_{-2.0} M_{\oplus}$ and, consequently, a density of $\rho_b = 0.795^{+0.290}_{-0.235} \text{ g cm}^{-3}$, it can be considered a warm Neptune-sized planet. Compared to other exoplanets of a similar mass range, TOI-1422 b is among the most inflated, and we expect this planet to have an extensive gaseous envelope that surrounds a core with a mass fraction around 10% – 25% of the total mass of the planet. The outer non-transiting planet candidate, TOI-1422 c, has an orbital period of $P_c = 29.29^{+0.21}_{-0.20}$ days, a minimum mass, $M_c \sin i$, of $11.1^{+2.6}_{-2.3} M_{\oplus}$, an equilibrium temperature of $T_{\text{eq},c} = 661 \pm 13$ K and, therefore, if confirmed, could be considered as another warm Neptune.

Key words. techniques: photometric – planetary systems – techniques: spectroscopic – techniques: radial velocities – stars: individual: TOI-1422 – methods: data analysis

1. Introduction

Exoplanetary science has expanded quickly from the simple detection of new worlds to their in-depth characterization. This characterization is especially feasible for planets orbiting bright stars on a plane almost aligned to our line of sight, meaning that their radius and mass can be derived by transit photometry and radial velocity (RV) measurements, respectively. The population of known transiting planets has increased significantly in the last two decades, mainly thanks to dedicated ground-based surveys, which were then followed by surveys from space that turned out to be much more efficient, considering the total number of discoveries.

Thus far, the *Kepler* and the K2 space missions (Borucki et al. 2010; Howell et al. 2014) have had a very important impact

on the exoplanet field by discovering thousands of confirmed and candidate planets, many of which are not amenable to RV follow-up due to the faintness of their host stars. The Transiting Exoplanet Survey Satellite (TESS; Ricker et al. 2014), currently at the end of its first extended mission and with a second one already proposed, was designed to target nearby and bright stars over a large portion of the sky (around 85% sky coverage during the primary mission alone) because such stars are easier to follow up by means of RV, and result in refined measurements of their own exoplanet masses, atmospheres, sizes, and therefore, densities. The opportunity to use a large exoplanet sample such as that of *Kepler*, which is based on homogeneous data and has minimal pollution from false positives (< 10%, Fressin et al. 2013), has allowed us to distinguish between several distinct exoplanet regimes (Weiss & Marcy 2014; Buchhave et al. 2014;

Zeng et al. 2019): the terrestrial-like planets ($R_p < 1.7 R_\oplus$), the gas dwarf planets with rocky cores and hydrogen–helium envelopes, the H₂O-dominated ices and fluid water worlds (both of the latter two classes have $1.7 R_\oplus < R_p < 3.9 R_\oplus$) and the ice or gas giant planets ($R_p > 3.9 R_\oplus$).

Planet occurrence around main-sequence stars has been investigated thanks to Doppler surveys (e.g. Cumming et al. 2008; Wright et al. 2012). In particular, the Keck Eta-Earth survey (Howard et al. 2010) and the CORALIE+HARPS survey (Mayor et al. 2011) first explored the domain of low-mass ($3\text{--}30 M_\oplus$) close-in ($P_{\text{orb}} \sim 50$ days) planets. These planets turned out to be an order of magnitude more common than giant planets.

Other studies for determining the occurrence rates of planets, based on the *Kepler* sample, agree that for planets with less than a 1-yr orbital period, their mean number per star is higher within the radius range $1 R_\oplus < R_p < 4 R_\oplus$ rather than the range $4 R_\oplus < R_p < 16 R_\oplus$, (Howard et al. 2012; Fressin et al. 2013; Petigura et al. 2013). The subsequent and gradual refinement of parent-star properties (especially thanks to high-resolution stellar spectra) revealed a clear bimodality of the radius distribution of close-in ($P < 100$ days), small-sized ($R_p < 4.0 R_\oplus$) planets orbiting bright, main-sequence solar-type stars (Petigura et al. 2017; Fulton & Petigura 2018; Van Eylen et al. 2018)¹. These two quite distinct populations were identified as ‘super-Earths’ ($R_p < 1.5 R_\oplus$) and ‘sub-Neptunes’ ($R_p = 2\text{--}3 R_\oplus$), which are also represented in the intermediate region ($R_p = 1.5\text{--}2 R_\oplus$) with fewer planets. However, it is better to stress that, since we do not know for sure what they are made of, the space of physical parameters (R_p , M_p), for which the previous terms apply, are not strictly defined.

The advantage of studying transiting planets is the possibility, in many cases, to measure both the planetary radius and mass, and therefore determine their density and bulk composition. Knowing the structural properties, one should be able to distinguish among the various scenarios of exoplanet formation and evolution. Unfortunately, theoretical models (e.g. Bitsch et al. 2019; Turbet et al. 2020) tell us that the mass-radius relationships for small planets present degeneracy due to the vastness of possible different compositions and amounts of rock, ice, and gas, especially in the transition between rocky super-Earths and Neptune-like planets (e.g. Miller-Ricci et al. 2009; Lozovsky et al. 2018). A detailed investigation of the mass-radius relation for small planets can be useful for throwing light on several open questions, such as the diversity of planet core masses and compositions, or where they form (in situ or beyond the snowline), and the existence of the radius gap. We refer the reader to the recent review by Biazzo et al. (2022) for an exhaustive discussion on this topic.

It is therefore clear how RV follow-up observations and planetary-mass measurements play an important role in understanding this process and why there is currently a tremendous effort in this field by many teams (e.g. KESPRINT: Gandolfi et al. 2018; HARPS-N consortium: Cloutier et al. 2020; NCORES: Armstrong et al. 2020; TESS-Keck Survey: Chontos et al. 2022; GAPS: Carleo et al. 2021) to confirm TESS small-planet candidates.

Probing the chemical composition of the atmosphere of a large number of sub-Neptune planets would also be helpful to unravel the skein. Various techniques (such as high-resolution spectroscopy, transmission, and emission spectroscopy) have

been implemented and applied successfully using the *Hubble* Space Telescope (HST) instruments or the high-resolution spectrographs mounted on large-class ground-based telescopes (e.g. CRILES: Snellen et al. 2010; HARPS: Wyttenbach et al. 2015; LDSS3C: Diamond-Lowe et al. 2018; GIANO: Brogi et al. 2018; CARMENES: Casasayas-Barris et al. 2019; HARPS-N: Pino et al. 2020; ESPRESSO: Borsa et al. 2021). Unfortunately, these techniques for probing the planetary atmospheres are currently effectively applicable only to giant planets, as we know only a few sub-Neptune planets for which the transmission-spectrum signal can be detected with a sufficient signal-to-noise ratio (S/N) that allows us to discriminate between different atmospheric models. The featureless transmission spectra of GJ 436 b (Knutson et al. 2014) and GJ 1214 b (Kreidberg et al. 2014) are emblematic.

The situation should improve soon thanks to the *James Webb* Space Telescope (JWST; Barstow et al. 2015), which is about to go into operation, and with the next generation of space-based and large ground-based telescopes (Ariel: Tinetti et al. 2021; ELT: Ramsay et al. 2021; TMT: Skidmore et al. 2015). In the meantime, it is important that we continue to work to uncover new exoplanets, especially those of small size ($R_p < 5 R_\oplus$) that orbit bright ($V < 11$ mag) main-sequence dwarf stars. This is currently possible thanks to the large number of planet candidates (more than 5000) that TESS is discovering at the present time. The recent detection of water vapour in the atmosphere of the super-Neptune TOI-674 b with the HST (Brande et al. 2022) is a successful example of this effort.

On the 6 November 2019, the TESS target star TIC 333473672 was officially named TOI-1422 (TESS Object of Interest; Guerrero et al. 2021), following the Data Validation Report Summary (DRS) produced by the TESS Science Processing Operations Center (SPOC; Jenkins et al. 2016) pipeline at the NASA Ames Research Center through the Transiting Planet Search (TPS; Jenkins 2002; Jenkins et al. 2010, 2020) and Data Validation (DV; Twicken et al. 2018, Li et al. 2019) modules. In particular, TOI-1422 01 was flagged as a potential planet with an orbital period of 13.0020 ± 0.0040 days, a transit depth of 1422 ± 94 ppm (parts per million), and a corresponding radius of $3.85 \pm 0.90 R_\oplus$, which is compatible with Neptune’s radius. The candidate passed all SPOC DV diagnostic tests, and, furthermore, all TIC (version 8) objects other than the target star were excluded as sources of the transit signal through the difference image centroid offsets (Twicken et al. 2018).

The long-term, multi-programme Global Architecture of Planetary Systems (GAPS; Covino et al. 2013; Poretti et al. 2016) exploits Doppler measurements taken with the High Accuracy Radial velocity Planet Searcher for the Northern hemisphere (HARPS-N; Cosentino et al. 2012) instrument at the Telescopio Nazionale *Galileo* (TNG) in La Palma (Spain). This high-resolution spectrograph (resolving power $R \approx 115\,000$) delivers the highest RV precision ($\sim 1 \text{ m s}^{-1}$) currently achievable in the northern hemisphere. One of the aims of the GAPS programme is to confirm and obtain an accurate mass determination of planets having an intermediate-mass between super-Earths and super-Neptunes; for this reason, TOI-1422 was selected for RV follow-up observations, which started in June 2020.

In the present work, we report the results of our measurements and analyses that allowed us to confirm TOI-1422 as a new planetary system. The paper is organized as follows: Sect. 2 contains the details of the instruments, and the photometric and RV measurements; the results of our analyses are presented in Sect. 3

¹ For a possible explanation of Fulton’s gap, see Modirrousta-Galian et al. (2020).

and discussed in Sect. 4; and we finally address the conclusions in Sect. 5.

2. Observations and data reduction

2.1. TESS photometry

Since late July 2018, TESS has observed more than 200 000 stars with its four wide-field optical Charged-Coupled Devices (CCD) cameras (24×96 degrees), each having a focal ratio of $f/1.4$ and a broad-band filter range between 600 and 1000 nm. The pre-selected target TIC 333473672 was observed in Sectors 16 and 17 between 11 September 2019 and 2 November 2019, and the first of a total of four transiting events were recorded on 19 September 2019. The two-minute cadence photometry of TOI-1422 from TESS spans a total of ≈ 50 days and to analyse it, we used the Presearch Data Conditioning Simple Aperture Photometry (PDC-SAP; Stumpe et al. 2012, 2014, Smith et al. 2012) light curve, which is provided by the TESS SPOC pipeline and retrieved through the Python package `lightkurve` (Lightkurve Collaboration 2018) from the Mikulski Archive for Space Telescopes (MAST). We jointly fitted the transit model and a Gaussian process (GP) using a simple (approximate) Matern kernel, which was implemented in the Python modelling tool `juliet`² (Espinoza et al. 2019) via `celerite` (Foreman-Mackey et al. 2017), of the form:

$$k(\tau_{i,j}) = \sigma_{\text{GP}}^2 M(\tau_{i,j}, \rho) + (\sigma_i^2 + \sigma_w^2) \delta_{i,j}, \quad (1)$$

where σ_i is the error bar of the i -th data point, σ_{GP} the amplitude of the GP in parts per million (ppm), σ_w an added jitter term (in ppm), $\delta_{i,j}$ the Kronecker's delta, $k(\tau_{i,j})$ the element i,j of the covariance matrix as a function of $\tau_{i,j} = |t_i - t_j|$, with t_i and t_j being the i,j GP regressors (i.e. the observing times), while

$$M(\tau_{i,j}, \rho) = (1 + 1/\epsilon) e^{-[1-\epsilon]\sqrt{3}\tau_{i,j}/\rho} + (1 - 1/\epsilon) e^{-[1+\epsilon]\sqrt{3}\tau_{i,j}/\rho} \quad (2)$$

is the kernel with its characteristic time scale ρ . The parameter ϵ controls the quality of the approximation since, in the limit $\epsilon \rightarrow 0$, Eq. (2) becomes the Matern-3/2 function. In `juliet`, the possible polluting sources inside the TESS aperture³ (Fig. 1), which might result in a smaller transit depth compared to the real one, are taken into account with a dilution factor (D) that, in this case, has been neglected because the PDC-SAP photometry is already corrected for dilution from other objects contained within the aperture using the Create Optimal Apertures (COA) module (Bryson et al. 2010, 2020)⁴. In order to efficiently sample the whole plausible zone in the (b, k) plane, where b is the impact parameter and k is the planet-to-star radius ratio, we used the (r_1, r_2) parametrization described in Espinoza (2018). This is the same approach that we adopted for the modelling of the transits in the joint analysis with the RVs (see Sect. 3.3). Moreover, here we make use of the limb-darkening parametrizations of Kipping (2013) for two-parameter limb-darkening laws ($q_1, q_2 \rightarrow u_1, u_2$).

The PDC-SAP light curve of TOI-1422 and its detrending are plotted in Fig. 2. We also analysed the SPOC SAP photometry (Twicken et al. 2010; Morris et al. 2020), which presents a small

² <https://juliet.readthedocs.io>

³ `tpfplotter` is a python package developed by J. Lillo-Box and publicly available on www.github.com/jlillo/tpfplotter.

⁴ Since the release of the light curve products from Year 2, the SPOC background estimation algorithm has been updated due to an over-correction bias, which was significant for dim and/or crowded targets. For this particular TOI, we estimated this over-correction to be negligible for the planetary radius estimation as it is significantly smaller than the transit depth uncertainty.

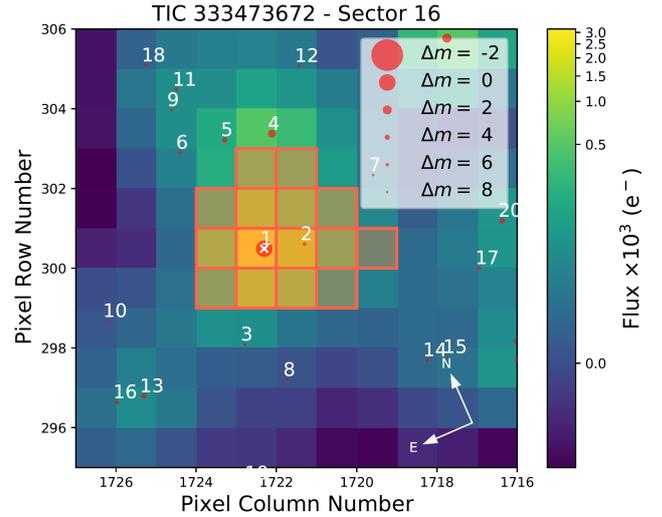


Fig. 1. Target pixel file from the TESS observation of Sector 16, made with `tpfplotter` (Aller et al. 2020) and centred on TOI-1422, which is marked with a white cross. The SPOC pipeline aperture is shown by shaded red squares, and the *Gaia* satellite eDR3 catalogue (Brown et al. 2018; Prusti et al. 2016) is also overlaid with symbol sizes proportional to the magnitude difference with TOI-1422. The difference image centroid locates the source of the transits within 1.89 ± 5 arcsec of the target star's location, as reported by the TicOffset for the multi-sector DV report for this system.

long-term variability that might be due to systematics, but no other feature or modulation can be discerned within the experimental uncertainties, aside from a possible single extra transit event, which is discussed at the end of Sect. 3.4, and a steep flux drop at the end of both the SAP and PDC-SAP light curves, which are probably due to high levels of background noise.

2.2. High-spatial resolution imaging – AstraLux

We observed TOI-1422 with the AstraLux high-spatial resolution camera (Hormuth et al. 2008), located at the 2.2 m telescope of the Calar Alto Observatory (CAHA, Almería, Spain) using the lucky-imaging technique. This technique obtains diffraction-limited images by acquiring thousands of short-exposure frames and selecting those with the highest Strehl ratio (Strehl 1902) to finally combine them into a co-added high-spatial resolution image. We observed this target on the night of 29 September 2021 under good weather conditions with a mean seeing of 1 arcsec, and obtained 50 000 frames with 20 ms exposure time in the Sloan Digital Sky Survey z filter (SDSSz), with a field of view windowed to 6×6 arcsec. The datacube was reduced by the instrument pipeline (Hormuth et al. 2008) and we selected the best quality 10% frames to produce the final high-resolution image. We obtained the sensitivity limits of the co-added image by using our own developed ASTRASENS package⁵ with the procedure described in Lillo-Box et al. (2012, 2014). The 5σ sensitivity curve is shown in Fig. 3. We could discard sources down to 0.2 arcsec with a magnitude contrast of $\Delta Z < 4$ mag, corresponding to a maximum contamination level of 2.5%. By using this high-spatial resolution image, we also estimated the probability of an undetected blended source. This probability (fully described in Lillo-Box et al. 2014) is called the blended source confidence (BSC). We used a python implementation of this approach (`bsc`, by J. Lillo-Box), which uses

⁵ <https://github.com/jlillo/astrasens>

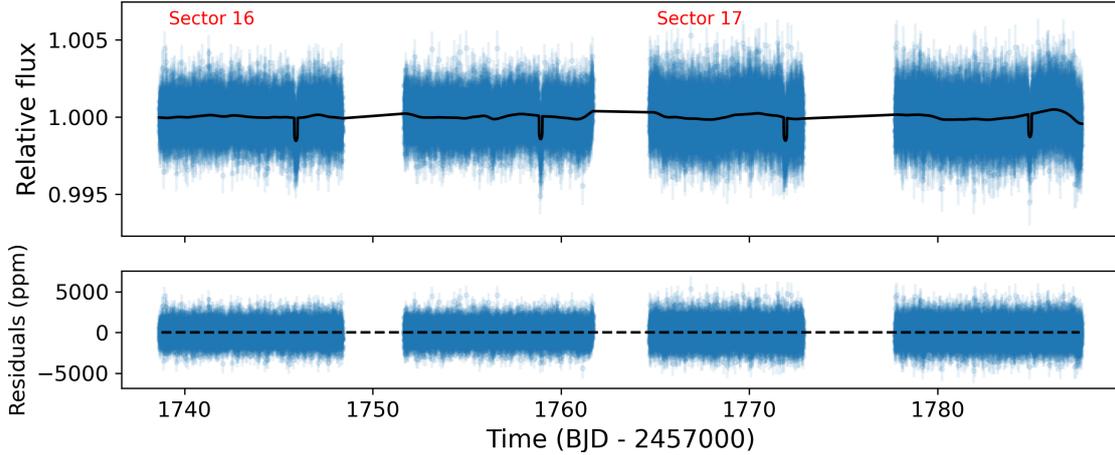


Fig. 2. Light curve of TOI-1422 as collected by TESS in Sectors 16 and 17 with a 2-min cadence. *Top panel:* light curve from the PDC-SAP pipeline. The black line represents the best-fit model obtained through GP detrending, as detailed in Sect. 2.1. *Bottom panel:* residuals of the best-fit model in parts per million.

the TRILEGAL⁶ galactic model (v1.6; Girardi et al. 2012) to retrieve a simulated source population of the region around the corresponding target⁷. This simulated population was used to compute the density of stars around the target position (radius $r = 1^\circ$) and derive the probability of chance alignment at a given contrast magnitude and separation. When applied to the TOI-1422 location, we used a maximum contrast magnitude of $\Delta m_{b,\max} = 6.97$ mag in the SDSSz passband, corresponding to the maximum contrast of a blended eclipsing binary that could mimic the observed transit depth of planet b (~ 1000 ppm). Thanks to our high-resolution image, we estimated the probability of an undetected blended source to be 0.28%. The probability of such an undetected source being an appropriate eclipsing binary was thus even lower and consequently, we could assume that the transit signal was not due to a blended eclipsing binary.

2.3. HARPS-N radial velocities

Between June 2020 and January 2022, we collected a total of 112 RV measurements of TOI-1422 with HARPS-N (Table A.1). The RVs were calculated using the TERRA pipeline (Anglada-Escudé & Butler 2012), version 1.8, through the YABI workflow interface (Hunter et al. 2012), which is maintained by the Italian center for Astronomical Archive (IA2). TERRA is an algorithm based on the template matching technique, and is preferred for the RVs retrieval in this paper over the standard Data Reduction Software (DRS) pipeline, which returned a slightly lower overall RV precision⁸ on this target. We used the RVs calculated using all the spectral orders, and from the full sample of RVs, we removed four points following Chauvenet’s criterion. TERRA RVs have an average measurement error of 2.6 m s^{-1} , a root mean square error of 4.5 m s^{-1} , and a $S/N \approx 35$, measured at a reference wavelength of 5500 \AA . A long linear trend is evident in HARPS-N RV data, as we discuss in Sect. 3.2.

TOI-1422 was also observed with the SOPHIE instrument, a stabilized échelle spectrograph mounted at the 193-cm Telescope of Observatoire de Haute-Provence in France (Perruchot et al. 2008, Bouchy, F. et al. 2013). However, for signals of low

⁶ <http://stev.oapd.inaf.it/cgi-bin/trilegal>

⁷ This is done in python by using the astrobase implementation by Bhatti et al. (2020).

⁸ For a comparison of the performances of TERRA vs. DRS see Perger et al. (2017).

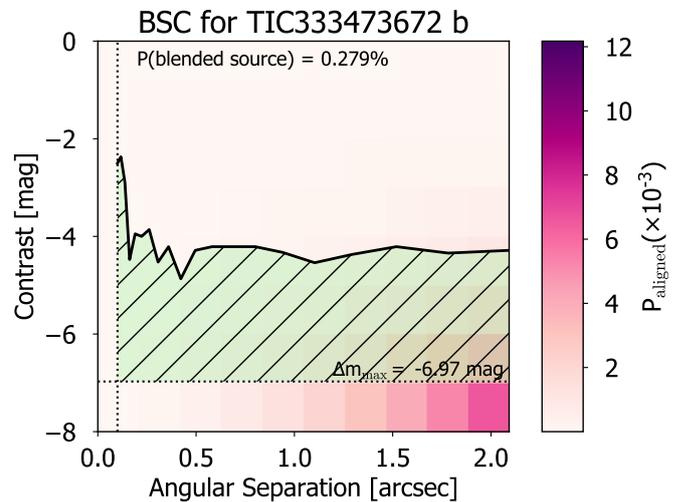


Fig. 3. Blended source confidence (BSC) curve from the AstraLux SDSSz image (solid black line). The colour on each angular separation and contrast bin represent the probability of a source aligned at the location of the target, based on the TRILEGAL model. The horizontal dotted line shows the maximum contrast of a blended binary that is capable of imitating the planet’s transit depth. The green region represents the regime that is not explored by the high-spatial resolution image. The BSC curve corresponds to the integration of P_{aligned} over this region.

semi-amplitudes such as those we discuss in this work, the RV measurements of SOPHIE, due to higher uncertainties compared to HARPS-N, do not increase the significance of the results presented in Sect. 5, and therefore have not been utilized.

3. System characterization

3.1. Parent star

From the co-added spectrum built from individual HARPS-N spectra extracted with the standard DRS pipeline, we derived the following atmospheric parameters of the planet’s host star TOI-1422: effective temperature T_{eff} , surface gravity $\log g$, microturbulence velocity ξ , iron abundance [Fe/H],

and rotational velocity $v \sin i_*$. For T_{eff} , $\log g$, ξ , and $[\text{Fe}/\text{H}]$, we applied a method based on equivalent widths of iron lines taken from [Biazzo et al. \(2015\)](#) and the spectral analysis package MOOG ([Snedden 1973](#); version 2017). The [Castelli & Kurucz \(2003\)](#) grid of model atmospheres was adopted. T_{eff} and ξ were derived by imposing that the abundance of Fe I was not dependent on the line excitation potentials and the reduced equivalent widths (i.e. EW/λ), respectively, while $\log g$ was obtained by imposing the Fe I/Fe II ionization equilibrium condition. The $v \sin i_*$ was measured with the same MOOG code, by applying the spectral synthesis of three regions around 5400, 6200, and 6700 Å, and adopting the same grid of model atmosphere after fixing the macroturbulence velocity to the value of 3.4 km s^{-1} from the relationship by [Doyle et al. \(2014\)](#). From these results, the star can be classified as a G2 V dwarf with a low projected rotation velocity $v \sin i_*$ of $1.9 \pm 0.8 \text{ km s}^{-1}$, implying a maximum rotation period of 27_{-8}^{+19} d at 1σ . Analogously, using an empirical relation based on the Full Width at Half Maximum (FWHM)⁹ derived by the HARPS-N DRS, we find $v \sin i_* \sim 2.2 \text{ km s}^{-1}$.

The field of TOI-1422 was also observed in 2004, 2006, and 2007 during the WASP transit-search survey ([Pollacco et al. 2006](#)). A total of 20 000 photometric data points were obtained by observing the field every ~ 15 min on clear nights, over spans of ~ 120 days in each year. We searched the data for any rotational modulation using the methods from [Maxted et al. \(2011\)](#) and found no significant periodicity between 1 and 100 days, with a 95%-confidence upper limit on the amplitude of 2 mmag. The TESS light curve shows no modulation either (Sect. 2.1), confirming that the star is rather magnetically quiet over a period of ~ 100 days.

Moreover, the spectrum of TOI-1422 clearly shows a lithium line at $\lambda = 6707.8 \text{ \AA}$. We therefore estimated the lithium abundance $\log A(\text{Li})_{\text{NLTE}}$ by measuring the lithium EW and considering our T_{eff} , $\log g$, ξ , and $[\text{Fe}/\text{H}]$ previously derived together with the NLTE corrections by [Lind et al. \(2009\)](#). The value of the lithium abundance is listed in Table 1 and its position in a $\log A(\text{Li})$ - T_{eff} diagram is compatible with the M67 open cluster *advanced age* (~ 4.5 Gyr; see [Pasquini et al. 2009](#)) in agreement with the star's low activity level. The physical parameters of TOI-1422 are also displayed in Table 1 and were determined with the EXOFASTv2 Bayesian code ([Eastman 2017](#); [Eastman et al. 2019](#)), by fitting the stellar spectral energy distribution (SED) and by employing the MESA Isochrones and Stellar Tracks ([Dotter 2016](#)) to more precisely constrain the stellar mass. In addition, in the table we report the stellar magnitudes used for the SED modelling, while the SED best fit is shown in Fig. 4. Gaussian priors were imposed on the *Gaia* eDR3 parallax ([Gaia Collaboration 2021](#)) as well as on the T_{eff} and $[\text{Fe}/\text{H}]$, as derived above from the analysis of the HARPS-N spectra. An upper limit was set on the V -band extinction, A_V , from reddening maps ([Schlegel et al. 1998](#); [Schlafly & Finkbeiner 2011](#)).

3.2. RV and activity indexes periodogram analysis

We computed the generalized Lomb-Scargle (GLS) periodogram for the HARPS-N RVs and different stellar activity indexes¹⁰

⁹ This relation was calibrated using a set of well-aligned transiting exoplanet systems, for which we could infer $v \sin i_*$ as equal to their equatorial velocities. We estimate the equatorial velocities from the stellar radii and rotational period, and correlated these values directly to the FWHMs.

¹⁰ The FWHM and the Bisector inverse span (BIS) are calculated using the cross correlation function (CCF) derived by the DRS pipeline. We

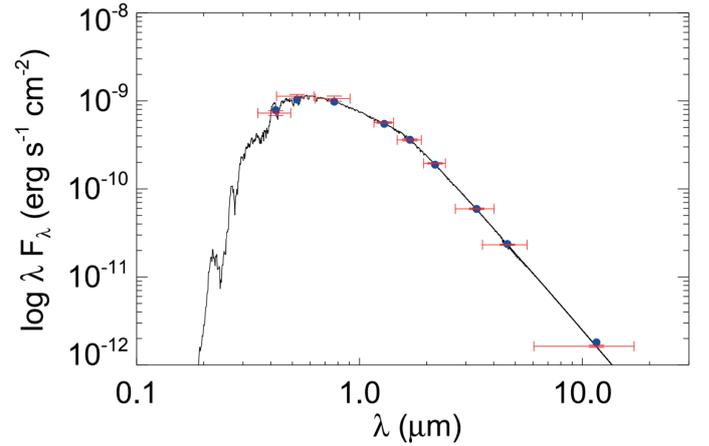


Fig. 4. Spectral energy distribution computed for TOI-1422, where the black curve is the most likely atmospheric stellar model and the blue dots correspond to the model fluxes over each passband. The horizontal and vertical red error bars represent, respectively, the effective width of the passbands and the reported photometric measurement uncertainties (refer to the magnitudes in Table 1).

using the Python package *astropy* v.4.3.1 ([Price-Whelan et al. 2018](#)). The periodogram of the RVs shows the main peak around 29 days, and a significant peak at 13 days (TOI-1422 b transiting period), after correcting for a linear trend of $\sim 4 \text{ m s}^{-1} \text{ yr}^{-1}$, observed in HARPS-N data. No index shows signs of the 29-day periodicity, but a linear trend is also present in the FWHM and $\log R'_{\text{HK}}$ (see Fig. D.1), with the former correlating the most with the RVs, unveiling a moderate Spearman coefficient ([Spearman 1904](#)) of 0.41 (p -value 0.01%). Therefore, in order to explain the nature of the main peak in the RVs, we present the GLS periodogram of these coefficients posterior to the removal of their linear trends in Fig. 5 (see Fig. D.2 for a closer look at the RVs panel), but again no trace of the 29-day signal is found. We also performed a GP regression analysis, using a quasi-periodic model, of the $\log R'_{\text{HK}}$ index corrected for the linear trend over the time series, and find no evidence of any particular periodic modulation in the posterior distribution of the periodic time-scale hyper-parameter. In short, there is no evidence pointing to a specific periodic rotation of the star TOI-1422, other than the tentative estimation from $v \sin i_*$.

A query from the *Gaia* eDR3 archive returns astrometric excess noise and renormalized unit weight error (RUWE) values of $80 \mu\text{as}$ and 1.09, respectively, for TOI-1422. Thus, the star is astrometrically quiet. The analysis of Sect. 2.2 rules out the existence of obvious sub-arcsec stellar companions, and no co-moving objects are present in *Gaia* eDR3 data in a 600 arcsec radius. The linear trend seen in the RV data, along with a few activity indexes, can therefore be explained by long star magnetic activity, rather than by the presence of a companion¹¹.

also analysed the chromospheric $\log R'_{\text{HK}}$ index, and additional activity diagnostics derived from the spectroscopic lines He I, Na I, Ca I, H α 06 and H α 16 as defined in the code ACTIN (<https://github.com/gomesdasilva/ACTIN> v.1.3.9, [Gomes da Silva et al. 2018](#)) which has been used for the calculation. In particular, the two H-alpha indices have 1.6 and 0.6 Å band-pass width, respectively.

¹¹ In this case, at a projected separation of 0.1 arcsec (~ 15 au at the distance of TOI-1422), the lower limit of the AstraLux imaging data, a maximum RV slope of the magnitude measured in this work would be produced by a companion of $\sim 30 M_{\text{Jup}}$ (i.e. either a very low-mass star or a massive sub-stellar companion).

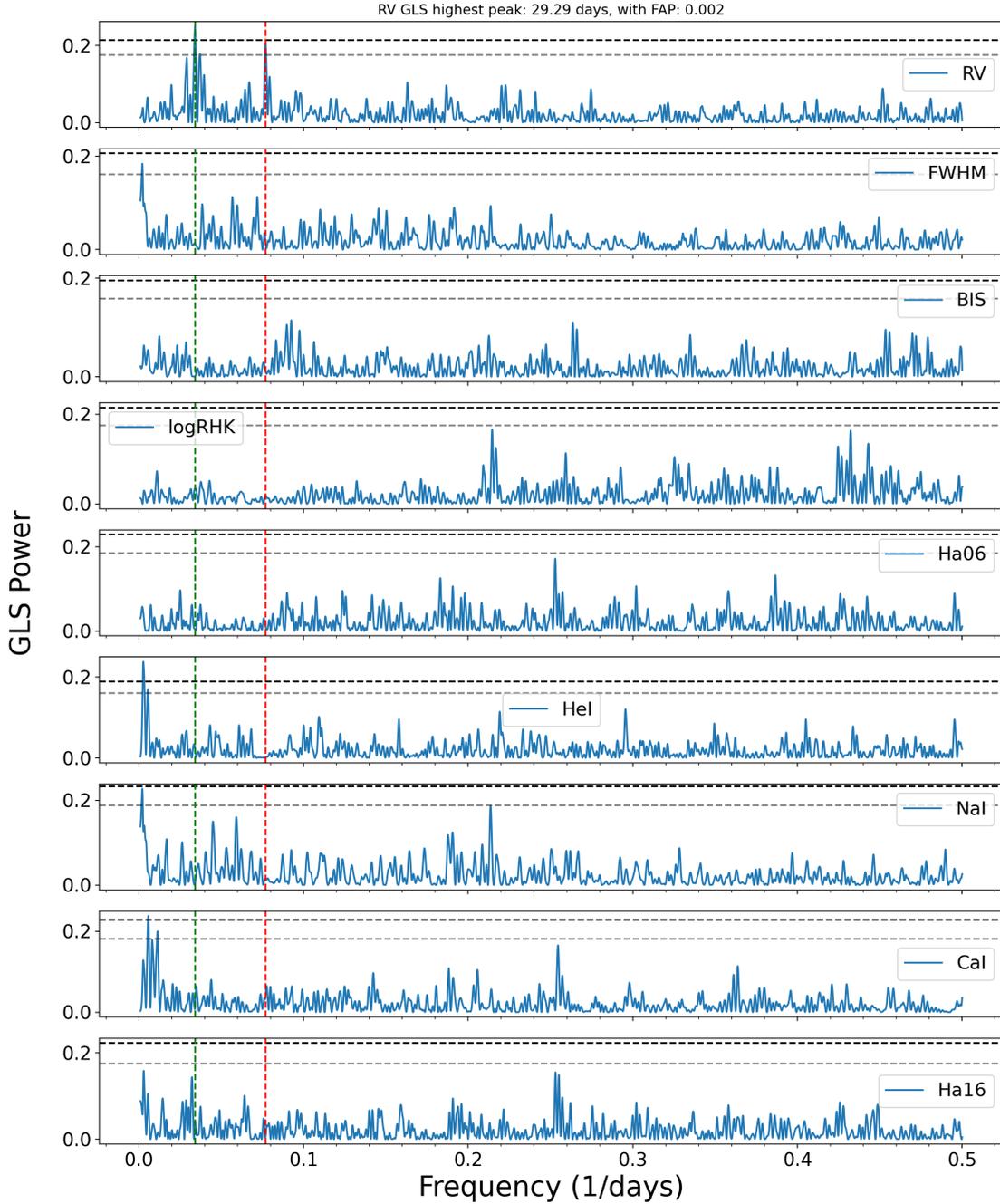


Fig. 5. GLS periodogram of HARPS-N RVs and of various activity indexes specified in the labels, after the removal of a linear trend (Sect. 3.2). The main peak of the RV GLS periodogram and that of the TOI-1422 b period are highlighted with a green and a red dashed line, respectively. They do not overlap with any of the peaks from the indexes, which in general do not suggest any clear stellar rotation period. The period corresponding to the highest peak in the RV GLS periodogram, and its False Alarm Probability (FAP), are written on the top of the first panel, while the horizontal dashed lines remark the 10% and 1% confidence levels (evaluated with the bootstrap method), respectively. The three peaks surrounding the RVs main frequency can all be explained as aliases of the 29-day signal due to the two highest frequencies of the window function (190 and 390.3 days, as shown in Fig. D.2 and Fig. D.3).

3.3. RV and photometry joint analysis

A joint transit and RV analysis was carried out with *juliet*, which employs different Python tools: *batman*¹² (Kreidberg 2015) for the modelling of transits, *RadVel*¹³ (Fulton et al. 2018) for the modelling of RVs, and stochastic processes, which are

treated as GPs with the packages *george*¹⁴ (Ambikasaran et al. 2015) and *celerite*¹⁵. The RV model that we used in *juliet* is the following:

$$M(t) = K(t) + \epsilon(t) + \bar{\mu} + At + B, \quad (3)$$

¹² <https://github.com/lkreidberg/batman>

¹³ <https://radvel.readthedocs.io>

¹⁴ <https://george.readthedocs.io>

¹⁵ <https://celerite.readthedocs.io>

Table 1. TOI-1422 parameters.

Parameter	Unit	Value	Source
Cross-identifications			
TOI	...	TOI-1422	TOI catalogue
TIC ID	...	333473672	TIC
<i>Tycho</i>	...	3235-00524-1	<i>Tycho</i>
2MASS ID	...	J23365789+3938218	2MASS
<i>Gaia</i> ID	...	1920333449169516288	<i>Gaia</i> eDR3
Astrometric properties			
R.A.	J2016	354.240817	<i>Gaia</i> eDR3
Dec	J2016	+39.639275	<i>Gaia</i> eDR3
Parallax	mas	6.4418 ± 0.0138	<i>Gaia</i> eDR3
μ_α	mas yr ⁻¹	-67.564 ± 0.015	<i>Gaia</i> eDR3
μ_δ	mas yr ⁻¹	-31.180 ± 0.011	<i>Gaia</i> eDR3
Distance	pc	154.56 ^{+0.037} _{-0.027}	VizieR
Photometric properties			
B_T	mag	11.31 ± 0.07	<i>Tycho</i>
V_T	mag	10.62 ± 0.05	<i>Tycho</i>
J	mag	9.585 ± 0.022	2MASS
H	mag	9.275 ± 0.030	2MASS
K_S	mag	9.190 ± 0.022	2MASS
i'	mag	10.311 ± 0.075	APASS
W_1	mag	9.161 ± 0.023	AllWISE
W_2	mag	9.201 ± 0.020	AllWISE
W_3	mag	9.161 ± 0.033	AllWISE
A_V	mag	< 0.077	This work
Stellar parameters			
L_\star	L_\odot	1.116 ± 0.037	This work
M_\star	M_\odot	0.981 ^{+0.062} _{-0.065}	This work
R_\star	R_\odot	1.019 ^{+0.014} _{-0.013}	This work
T_{eff}	K	5840 ± 62	This work
$\log g_\star$	cgs	4.41 ± 0.11	This work
ξ	km s ⁻¹	0.89 ± 0.07	This work
[Fe/H]	dex	-0.09 ± 0.07	This work
Spectral type ^(a)		G2 V	This work
ρ_\star	g cm ⁻³	1.3 ± 0.1	This work
$\nu \sin i_\star$	km s ⁻¹	1.7 ± 0.4	This work
$\log A(\text{Li})_{\text{NLTE}}$		1.97 ± 0.05	This work
$\log R'_{\text{HK}}$	dex	-4.95 ± 0.03	This work
Age	Gyr	5.1 ^{+3.9} _{-3.1}	This work

Notes. ^(a)Spectral type defined according to the stellar spectral classification of Gray & Corbally (2009).

References. TESS Primary Mission TOI catalogue (Guerrero et al. 2021); TIC (Stassun et al. 2018; Stassun et al. 2019); *Tycho* (Høg et al. 2000); 2MASS (Skrutskie et al. 2006); *Gaia* eDR3 (Brown et al. 2021); AllWISE (Cutri et al. 2021); APASS (Henden et al. 2015); VizieR Online Data catalogue (Bailer-Jones et al. 2021).

where $\epsilon(t)$ is a noise model for the HARPS-N instrument, here assumed to be white-Gaussian noise, in other words $\epsilon(t) \approx N(0, \sigma(t)^2 + \sigma_w^2)$, with $\sigma(t)^2$ being the formal uncertainty of the RV point at time t , σ_w^2 being an added jitter term, and $N(\mu, \sigma^2)$ denoting a normal distribution with mean μ and variance σ^2 . $K(t)$ is the Keplerian model of the RV star perturbations due to the orbiting planet, $\bar{\mu}$ is the systemic velocity linked to the instrument, and the coefficients A , B (also referred to as RV slope and RV intercept) represent an additional linear trend used for modelling non-Keplerian signals with a period longer than the observation span. For a total number of data points N , we assumed the model likelihood to follow the likelihood of an

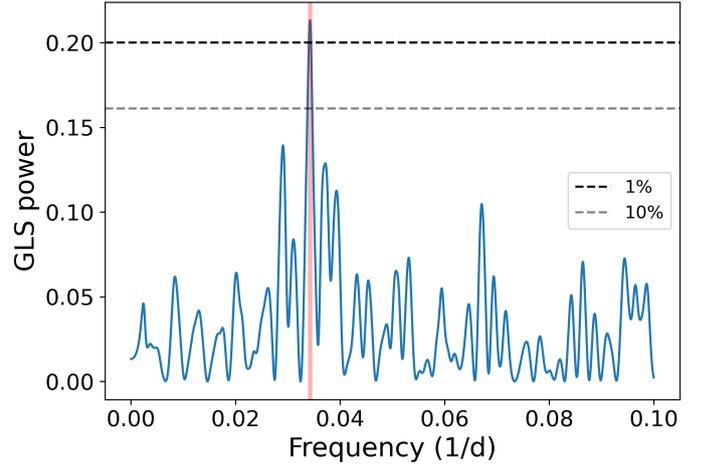


Fig. 6. GLS periodogram of the transiting one-planet model RV residuals. The main peak is highlighted in red and corresponds to a period of 29.2 days, with a FAP of 0.45% (evaluated with the bootstrap method), while the horizontal dashed lines show the 10% and 1% confidence levels.

N -dimensional multi-variate Gaussian:

$$\ln p(\mathbf{y}|\boldsymbol{\theta}) = -\frac{1}{2}[N \ln 2\pi + \ln |\Sigma| + \mathbf{r}^T \Sigma^{-1} \mathbf{r}], \quad (4)$$

where \mathbf{y} and $\boldsymbol{\theta}$ are vectors containing, respectively, all the RV data points and instrumental parameters, while \mathbf{r} is the residual vector given by

$$\mathbf{r}(t_i) = \mathbf{y}(t_i) - \mathbf{M}(t). \quad (5)$$

The elements of the covariance matrix Σ are:

$$\Sigma(t_i, t_j) = k(\mu_i, \mu_j) + (\sigma_w^2 + \sigma_t^2)\delta_{i,t_j}, \quad (6)$$

with k equal to any GP kernel model, or zero for a pure white-noise one. In order to estimate the Bayesian posteriors and evidence, \mathcal{Z} , of different models, we used the dynamic nested sampling package *dynesty* (Speagle 2020), which adaptively allocates samples based on a posterior structure and, at the same time, estimates evidence and sampling from multi-modal distributions. In general, dynamic nested sampling algorithms sample a dynamic number of live points from the prior ‘volume’ and sequentially replace the point with the lowest likelihood with a new one, while updating the Bayesian evidence by the difference $\Delta\mathcal{Z}$. Usually, the stopping criterion is a defined value of $\Delta\mathcal{Z}$, below which the algorithm is said to have converged ($\Delta\mathcal{Z} \approx 0.5$). However, here we used the default criterion described in Sect. 3.4 of Speagle (2020).

In order to reveal the transiting object suggested by the TESS light curve, we first ran the RV and photometry joint analysis with a simple one-planet model, using the parameters in the DVR produced by the SPOC pipeline as transit-related priors, both with a fixed null and uniformly-sampled eccentricity via the parametrization $S_1 = \sqrt{e} \sin \omega$, $S_2 = \sqrt{e} \cos \omega$, which is described in Eastman et al. (2013). All the priors are defined in Table B.1. In particular, we set Gaussian priors on both the limb-darkening coefficients (Claret 2017) and the star mean density ρ_\star (Sect. 3.1), which was implemented here instead of the scaled semi-major axis, a/R_\star , because the latter can be recovered using Kepler’s third law using only the period of the respective planet, which is a direct result of any *juliet* run. In this way, from

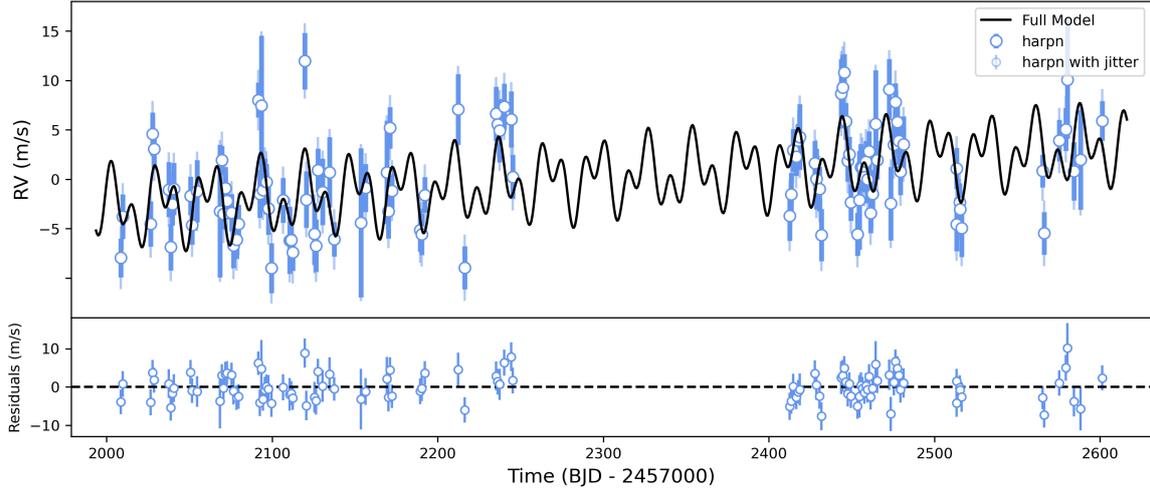


Fig. 7. RV measurements of TOI-1422 versus time are shown on the *top panel*, while their residuals over the model fit are in the *bottom panel*. The circles with blue error bars are the RV data taken with HARPS-N. The large and small error bars indicate σ_t and σ_w (the added jitter term), respectively. In the top panel, the black line represents the two-planet model fit.

the single value of ρ_\star we can evenly derive a/R_\star in the case of multiple planets.

The best one-planet RV model fit is found with $e = 0$ ($\Delta \ln \mathcal{Z}_{e_b \neq 0}^{e_b=0} = 0.7$), but the scatter of the residuals is higher than the average photon-noise uncertainties for this kind of star. In fact, the same peak of 29 days, which was found in the RV GLS periodogram, is also distinctly found in the residuals of the transiting one-planet model (see Fig. 6). Consequently, we proceeded to test two-planet models, whose priors are summed in Table B.2. Since they have comparable statistical significance ($\Delta \ln \mathcal{Z}_{e_{b,c} \neq 0}^{e_{b,c}=0} = 0.4$), we use the results of the eccentric model for the rest of the paper. The two-planet eccentric model is plotted on top of the RVs in Fig. 7, along with its residuals. TOI-1422 b RV semi-amplitude and orbital period are found to be $K_b = 2.47_{-0.46}^{+0.50} \text{ m s}^{-1}$ and $P_b = 12.9972 \pm 0.0006$ days, respectively. The second planet, candidate TOI-1422 c, has an RV semi-amplitude of $K_c = 2.36_{-0.40}^{+0.42} \text{ m s}^{-1}$, orbital period of $P_c = 29.29_{-0.20}^{+0.21}$ days and $T_{0,c} = 2458776.6 \pm 4.6$ BJD (see the posteriors in Fig. C.1 and Table B.3). The eccentricities turn out to be $e_b = 0.04_{-0.03}^{+0.05}$ and $e_c = 0.14_{-0.10}^{+0.17}$, but it is important to note that when they are fixed to zero, the orbital parameters of TOI-1422 b and TOI-1422 c remain, within $1\text{-}\sigma$, compatible with those of the eccentric model.

3.4. Results

TOI-1422 c's orbital period explains both the main peak found in the residuals of the one-planet model (Fig. 6) and in the RV GLS periodogram (Fig. 5); it is also in 9:4 orbital resonance with the first planet. The difference between the Bayesian evidence of the two-planet eccentric model and the one-planet model ($\Delta \ln \mathcal{Z}_{1p}^{2p} = 5.1$) is barely above the *very strong* evidence threshold defined in Kass & Raftery (1995) ($\Delta \ln \mathcal{Z} > 5$), so even if the existence of candidate planet c remains unproven, we believe the two-planet model is currently the better one to explain the 29-day signal observed in the RVs, due to the lack of evidence of star activity.

Furthermore, the two-planet analysis was replicated with different numbers of data points in order to understand how and if new measurements were impacting the significance of the

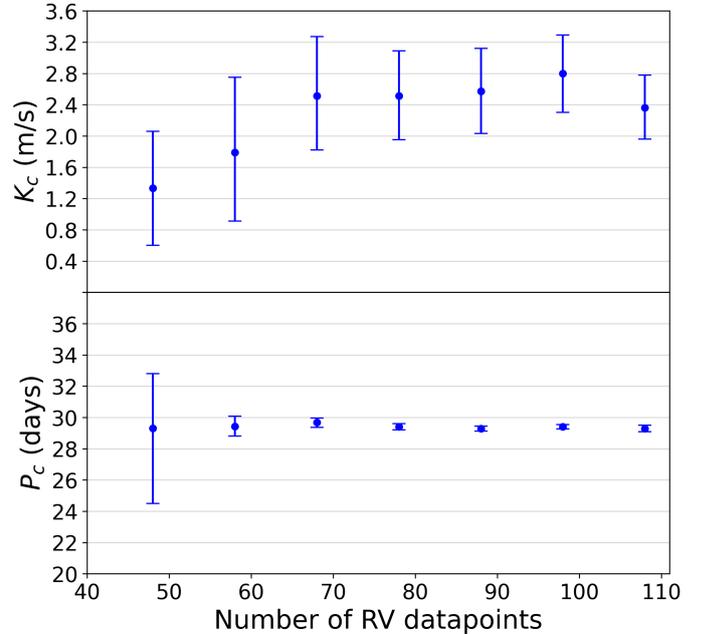


Fig. 8. RV semi-amplitude K and orbital period P , along with their $1\text{-}\sigma$ error bars, for candidate planet c, as functions of the number of data points used for the two-planet eccentric model analysis with *juliet*.

second planet detection. As shown in Fig. 8, both the RV semi-amplitude and the period seem to stabilize after ≈ 60 measurements, which matches the beginning of the second observation season, while the significance of the 29-day peak also grows (Fig. D.4). It is noteworthy to mention that the GLS periodogram of the residuals of the two-planet model does not show peaks below 50% FAP, and hence does not suggest the presence of additional detectable signals.

A phase-folded plot of both the transit and the RVs is shown in Fig. 9 for the eccentric two-planet model. The radius for TOI-1422 b was calculated with the transformations provided by Espinoza (2018) and, using the stellar radius from Sect. 3.1, its revised value turns out to be $R_b = 3.96_{-0.11}^{+0.13} R_\oplus$. Using the stellar radius from Table 1, we derived the mass of both objects to be

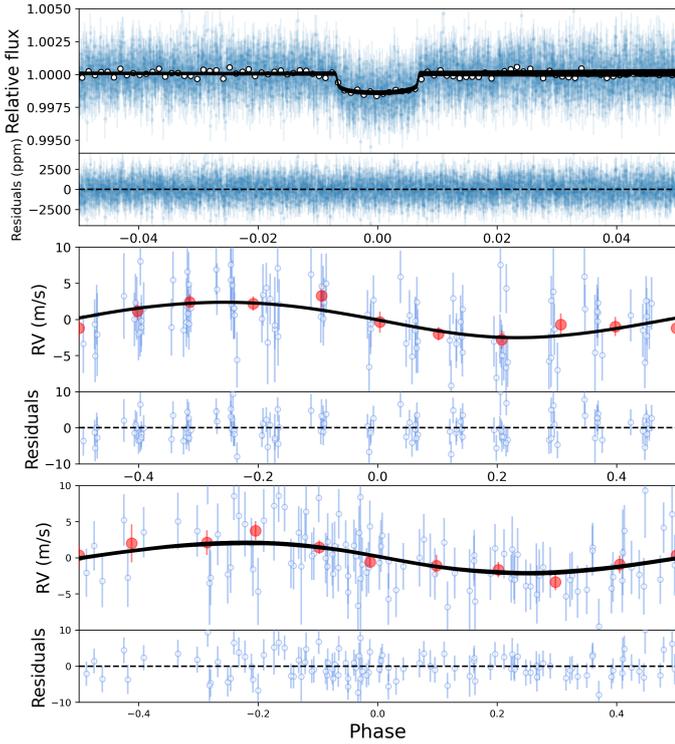


Fig. 9. TESS light curve and RV curves phase-folded. *Top panel:* TOI-1422 b transit, compared to the best-fitting model. *Bottom panels:* HARPS-N RV data phase-folded to the period of planet b (*middle*) and candidate c (*bottom*), along with their residuals over the model. The red circles represent the average value of phased RV data points.

$M_b = 9.0^{+2.3}_{-2.0} M_\oplus$ and $M_c \sin i_c = 11.1^{+2.6}_{-2.3} M_\oplus$. Their final parameters are reported in Table 2. An independent joint analysis of the HARPS-N RVs and TESS photometry, after the transits were normalized through a local linear fitting, was also performed with a DE-MCMC method (Eastman et al. 2013, 2019), following the same implementation as in Bonomo et al. (2014, 2015). The obtained results are consistent, within $1-\sigma$, with those reported in Table 2.

In order to evaluate possible transit time variations (TTVs) due to the influence of candidate TOI-1422 c over TOI-1422 b, we plot the four mid-transit times minus their expected values (based on the two-planet eccentric model) in Fig. 10, along with different TTV predictions made with the code described in Agol & Deck (2016). Unfortunately, there are not enough transits to draw any conclusions, as all the delays are compatible with zero within $1-\sigma$. Therefore, further precise monitoring of TOI-1422 b transits is encouraged in order to confirm the existence of TOI-1422 c and, overall, better characterize the planetary system.

3.5. Other transit events

In the search for TOI-1422 c transits, we found a possible single transit-like event around 2 458 756.35 BTJD days, as shown in Fig. 11, which cannot be related to either TOI-1422 b or TOI-1422 c. We fitted this potential transit using the light curve from the pipeline PATHOS (Nardiello et al. 2019) and retrieved a possible radius of $R_d = 2.82^{+0.38}_{-0.05} R_\oplus$, which is compatible with the transit depth observed in the PDC-SAP and SAP light curves as well. The duration of the transit suggests an orbital period longer than that for TOI-1422 c, but this is very uncertain, while the lack of other transits in the TESS light curve suggests an

Table 2. Best-fit median values, with upper and lower 68% credibility bands as errors, of the fitted and derived parameters for TOI-1422 b and TOI-1422 c, as extracted from the posterior distribution of the two-planet eccentric model (Table B.3 and Fig. C.1).

	TOI-1422 b	TOI-1422 c
Transit and orbital parameters		
K (m s^{-1})	$2.47^{+0.50}_{-0.46}$	$2.36^{+0.42}_{-0.40}$
P_{orb} (days)	12.9972 ± 0.0006	$29.29^{+0.21}_{-0.20}$
T_0 (BJD)	$2\,458\,745.9205^{+0.0012}_{-0.0011}$	$2\,458\,776.6^{+4.6}_{-4.5}$
T_{14} (hours)	4.52 ± 0.16	–
R_p/R_\star	$0.0356^{+0.0007}_{-0.0005}$	–
b	$0.19^{+0.11}_{-0.10}$	–
i (deg)	$89.52^{+0.26}_{-0.28}$	–
a/R_\star	$22.72^{+0.31}_{-0.40}$	$39.05^{+0.50}_{-0.73}$
q_1	$0.28^{+0.11}_{-0.08}$	–
q_2	$0.30^{+0.05}_{-0.05}$	–
$\sqrt{e} \sin \omega$	$0.018^{+0.108}_{-0.095}$	$0.120^{+0.221}_{-0.233}$
$\sqrt{e} \cos \omega$	$-0.149^{+0.153}_{-0.128}$	$-0.070^{+0.349}_{-0.304}$
Derived parameters		
M_p (M_\oplus)	$9.0^{+2.3}_{-2.0}$	–
$M_p \sin i$ (M_\oplus)	–	$11.1^{+2.6}_{-2.3}$
R_p (R_\oplus)	$3.96^{+0.13}_{-0.11}$	–
ρ_p (g cm^{-3})	$0.795^{+0.290}_{-0.235}$	–
$\log g_p$ (cgs)	$2.75^{+0.08}_{-0.14}$	–
a (AU)	0.108 ± 0.003	0.185 ± 0.006
$T_{\text{eq}}^{(\ddagger)}$ (K)	867 ± 17	661 ± 13
u_1	$0.32^{+0.12}_{-0.10}$	–
u_2	$0.21^{+0.10}_{-0.08}$	–
e	$0.04^{+0.05}_{-0.03}$	$0.14^{+0.17}_{-0.10}$
ω (deg)	153^{+20}_{-56}	99^{+63}_{-64}

Notes. ^(\ddagger) This is the equilibrium temperature for a zero Bond albedo and uniform heat redistribution to the night side.

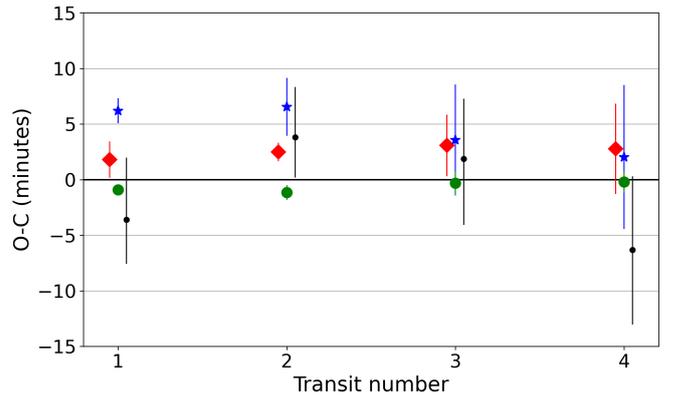


Fig. 10. Residuals for the mid-transit timings of TOI-1422 b versus a linear ephemeris, with $1-\sigma$ error bars, are plotted in black. The green circles, red diamonds, and blue stars represent TTV predictions in the cases of null, average, or maximum eccentricities, respectively, with the error bars showing the uncertainty due to $T_{0,c}$ (see Table 2). The points have been slightly shifted on the x-axis to allow for more visibility.

orbital period between 17 and 22, or longer than, 35 days, thus incompatible with that of TOI-1422 c. PATHOS is a PSF-based approach to TESS data that minimizes the dilution effects in crowded environments, and here it is utilized to extract high-precision photometry of TOI-1422 to independently confirm the

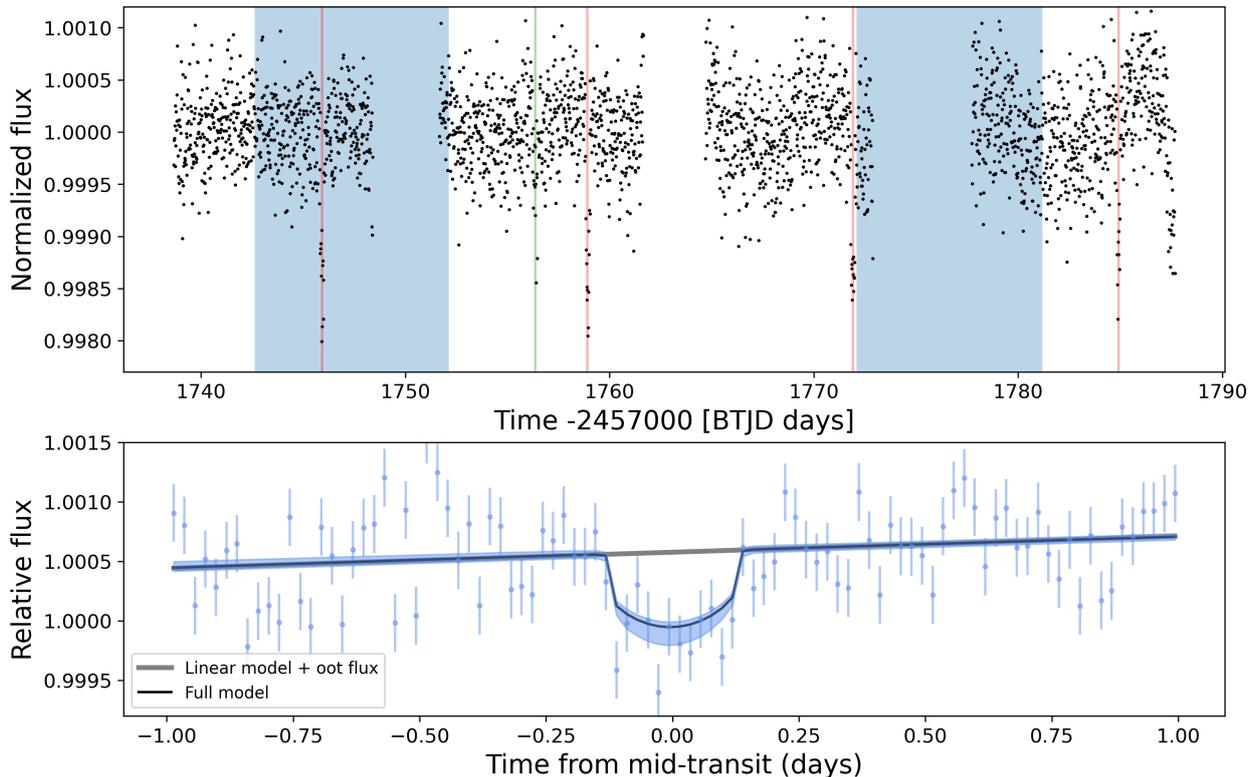


Fig. 11. PDC-SAP and PATHOS light curves. *Top panel:* TOI-1422 b transits highlighted in red in the PDC-SAP light curve, and the expected TOI-1422 c transits, with their uncertainties, highlighted in blue. A single planetary-transit event is also marked with a vertical line green, and is discussed at the end of Sect. 3.4). *Bottom panel:* Single transit-like event as seen in the PATHOS light curve and the corresponding fit.

presence of this transit even after the application of a different neighbour-subtraction technique. Neither the single transit nor TOI-1422 b transits show correlation with the X,Y pixels and the sky background signal (Fig. D.5), and the single transit depth also does not change with different photometric apertures (Fig. D.6). Nevertheless, the three-planet model for the joint transit-RV analysis is not statistically significant and the lack of other transits makes the suggestion of another candidate impossible to justify.

However, no transit compatible with the expected $T_{0,c}$ and P_c evaluated with the RV and photometry joint analysis, was found in the SPOC (both SAP and PDC-SAP) light curves, even though a small part of the supposed transiting window was missed by TESS. When we take into account both the time-span of the TESS light curve and TOI-1422 c expected (non-grazing) transit duration, the probability that such transits would have been missed can be estimated to be around 1% and 7%, with 1σ and 3σ uncertainty, respectively, on $T_{0,c}$. Other than misaligned orbits, another possible explanation for the lack of TOI-1422 c transits is that despite its mass, which is greater than that of planet b, its size could be much smaller (similar to the high-density sub-Neptune, BD+20594b of Espinoza et al. 2016), as any object with a radius approximately below $2.8R_{\oplus}$ might be disguised in the light curve noise (as proven by the, so far undetected and uncertain, single transit-like event). Ultimately, it remains unknown if candidate planet c is transiting or not, so further high-precision long photometric follow-up observations will be important to clear up this possibility, along with the nature of the single transit event. The new TESS observations of this target, during Sector 57, are definitely welcome as they might shed some light on both matters.

4. Discussion

4.1. Orbital resonance

As we have seen, candidate c is within $1-\sigma$, in 9:4 orbital resonance with planet b. This is likely coincidental since the resonance is fifth-order, and thus very weak, unless one of the planets is quite eccentric¹⁶ or the mutual inclination is high. The exact 9:4 (or 2.25) resonance is within uncertainty, perhaps only because the uncertainty of the orbital period of TOI-1422 c is large compared to the tight period uncertainties of transiting planets. As a matter of fact, period ratios a little above two have been found within many exoplanetary systems (Winn & Fabrycky 2015), but it is also possible that the 9:4 resonance is actually the result of a resonant chain of three planets in first-order 3:2 resonances among each other, with the middle one yet to be seen. If that is the case, since the period ratios of Kepler planets near first-order resonances are usually slightly wide of resonance, the likely orbital period for this unknown exoplanet would be slightly more than 19.5 days, and thus compatible with the observed single transit discussed in Sect. 3.4. Given this orbital period and assuming that an RV semi-amplitude roughly up to 2 m s^{-1} might be hidden in the residuals of the two-planet model, this middle object should not have a mass higher than $\approx 8 M_{\oplus}$, or a density higher than $\approx 2 \text{ g cm}^{-3}$.

¹⁶ We note that, even with the e 's suggested by the eccentric fits, which are unusually high compared to most multi-transiting planetary systems according to Xie et al. (2016), the 9:4 would not be as strong as a first-order resonance.

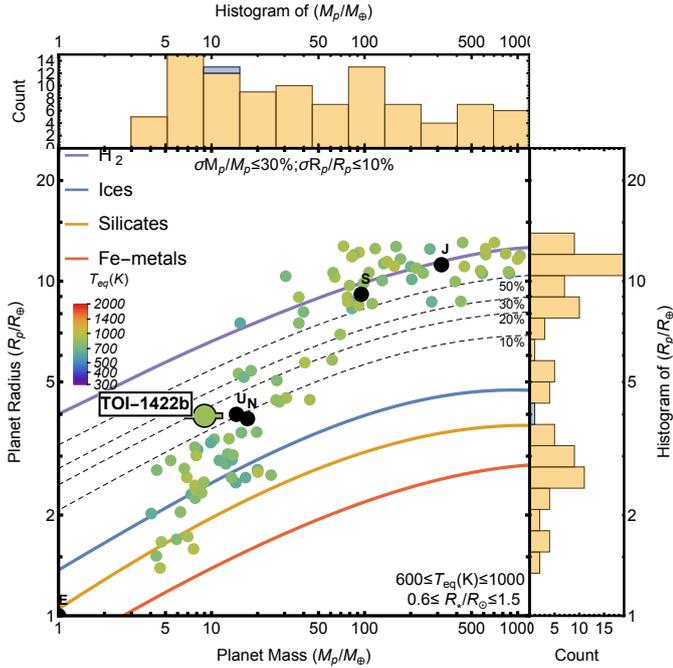


Fig. 12. Planetary masses and radii of the known transiting exoplanets (values taken from the Transiting Extrasolar Planet catalogue, TEP-Cat, which is available at <http://www.astro.keele.ac.uk/jkt/tepcat/> catalogue; Southworth 2010, 2011) with equilibrium temperature T_{eq} between 600 and 1000 K and host star radius between 0.6 and 1.5 R_{\odot} . Different lines correspond to different mass fractions of relatively cold hydrogen envelopes. The *ice giants* of the Solar System are displayed in filled black circles. TOI-1422 b is on the low-density envelope of planets with precise mass and/or radius estimations ($\sigma M_p/M_p \leq 30\%$; $\sigma R_p/R_p \leq 10\%$), one of the reasons that make it potentially valuable for transit spectroscopy.

4.2. Mass-radius diagram and internal structure of planet b

TOI-1422 b is one of the puffer planets with a density of $\sim 0.8 \text{ g cm}^{-3}$, which is close to that of Saturn and, therefore, lower than most exoplanets in this mass range. It lies towards the upper-left corner of the mass-radius diagram (Fig. 12), making it very similar to Kepler-36 c (Vissapragada et al. 2020) and especially to Kepler-11 e (Lissauer et al. 2013), which even shares the same kind of host star but is on a longer orbit. On one hand, it has a similar radius compared to Neptune and Uranus in our solar system, but on the other hand, its mass is only about 50–60% that of our ice giants. Thus, an extensive gaseous envelope, surrounding a massive core, is expected to be found in TOI-1422 b. More precisely, the mass fraction of this envelope is expected to be around 10–25% of the total mass of the planet (using the equations of state from Becker et al. 2014), suggesting that the atmosphere has not been blown away by the stellar wind. The nature of this extensive envelope as well as its core requires further investigation. For this purpose, we assess the expected S/N of the JWST/NIRISS measurements¹⁷ of TOI-1422 b transits compared to planets of similar sizes, by evaluating the transmission spectroscopy metric (TSM) defined in Kempton et al. (2018):

$$\text{TSM} = (\text{Scale factor}) \times \frac{R_{\oplus}^3 T_{\text{eq}}}{M_{\oplus} R_{\star}^2} \times 10^{-0.2J}, \quad (7)$$

¹⁷ From a 10-h observing programme assuming a cloud-free, solar-metallicity, H_2 -dominated atmosphere.

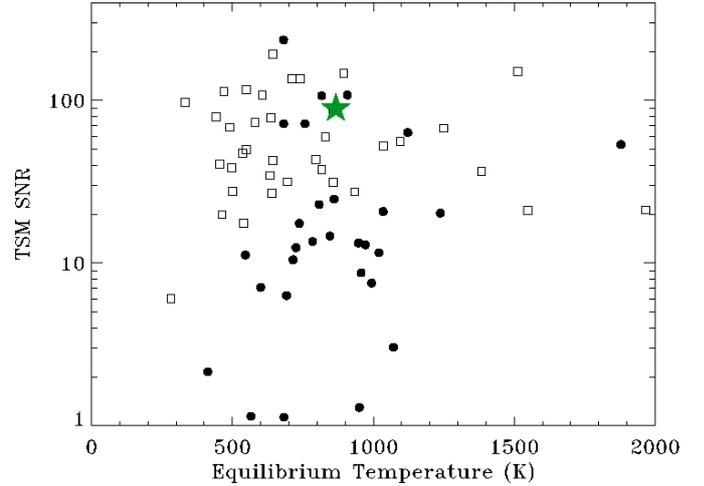


Fig. 13. Transmission spectroscopy observations (TSM) values with the JWST over the equilibrium temperature for planets with a measured mass in the radius range $2.75 < R_{\oplus} < 4.0$, including TOI-1422 b (green star). Filled black dots and empty squares identify the sample of planets around stars with $T_{\text{eff}} > 5400 \text{ K}$ and $T_{\text{eff}} < 5400 \text{ K}$, respectively.

where the scale factor is a dimensionless normalization constant, equal to 1.28 for planets with $2.75 < R_{\oplus} < 4.0$, and J is the apparent magnitude of the host star in the J band (a filter that is near the middle of the NIRISS bandpass). As a result (Fig. 13), TOI-1422 b ranks fourth¹⁸ among Neptunes ($2.75 < R_{\oplus} < 4.0$) orbiting G-F dwarfs ($T_{\text{eff}} > 5400 \text{ K}$), but being the one with the lowest density, it is definitely an interesting candidate for atmospheric characterization by the JWST.

5. Conclusions

In this paper, we have confirmed the planetary nature of the TESS transiting planet TOI-1422 b, which turns out to be a low-density and warm Neptune-sized planet orbiting an astrometrically, and overall magnetically, quiet G2 V star. Therefore, TOI-1422 b is the latest addition to the low-populated range of exoplanets with the size of Neptune, but with Saturn-like density. In order to well constrain the mass of TOI-1422 b, a long RV monitoring with more than a hundred observations was necessary with the HARPS-N instrument at the TNG in La Palma, which resulted in fully characterized orbital and physical parameters of this new planetary system. On top of that, our RV measurements also suggest the presence in the system of a possibly non-transiting, heavier candidate planet, TOI-1422 c, in a weak 9:4 orbital resonance with its inner brother, which will require further study to validate.

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¹⁸ Following TOI-561 c (Lacedelli et al. 2020, 2022), HD 136352 c (Kane et al. 2020; Delrez et al. 2021) and HD 63935 b (Scarsdale et al. 2021)

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Appendix A: HARPS-N RV datapoints

Table A.1. HARPS-N RV data points and activity indexes (used in Fig. 5) obtained with the TERRA reduction pipeline between June 8, 2020 and January 21, 2022. The four lines in bold highlight the RV data points that have been removed because they do not fit Chauvenet's criterion.

BJD _{UTC} -2457000[days]	RV	$\pm 1\sigma_{RV}$	FWHM	BIS ^(†)	Exp. ^(*)	S/N	$I_{Ca\ ii}$	$I_{H\alpha 06}$	$I_{He\ i}$	$I_{Na\ i}$	$I_{Ca\ i}$	$I_{H\alpha 16}$
	[m s ⁻¹]		–	–	[sec]	–	–	–	–	–	–	–
2008.69349316	-7.95	1.95	7174.86	-7.56	900	42.8	0.549907	0.084427	0.097028	0.180378	0.527652	0.683496
2009.71160774	-3.78	2.25	7181.28	-6.09	900	34.3	0.555074	0.078803	0.097526	0.179596	0.522912	0.63963
2026.66187880	-4.51	2.31	7164.91	0.894	900	44.2	0.554022	0.082134	0.100171	0.187731	0.505988	0.687073
2027.72062839	4.586	2.2	7153.54	-4.7	900	36.4	0.558749	0.083288	0.107005	0.187897	0.530667	0.687811
2028.69301741	3.085	2.06	7178.27	-6.91	900	39.3	0.587418	0.078941	0.098429	0.181754	0.53219	0.657997
2037.70925340	-1.04	2.78	7190.11	1.317	900	27.1	0.588273	0.087717	0.10143	0.184427	0.533928	0.670313
2038.71004788	-6.86	2.35	7174.7	-12.8	900	33.8	0.589738	0.08641	0.102117	0.18419	0.531931	0.671326
2039.71645615	-2.51	2.17	7176.79	-5.84	900	40.5	0.590585	0.078021	0.099401	0.182083	0.530063	0.658114
2040.70404346	-0.98	2.65	7182.67	-18.1	900	31.6	0.593109	0.085039	0.099033	0.182093	0.528559	0.650582
2050.69789104	-1.68	1.94	7172.47	-1.01	900	40.2	0.594075	0.087503	0.099635	0.183098	0.534144	0.666092
2051.69861363	-4.63	1.99	7177.72	-11.5	900	38.6	0.591485	0.076251	0.099171	0.182165	0.525447	0.654697
2054.72404480	-1.22	3.15	7162.98	-4.59	900	30.1	0.564703	0.094168	0.100699	0.182831	0.523618	0.663779
2068.61577511	-3.21	6.73	7165.8	-6.58	900	12.7	0.584758	0.089195	0.098718	0.179674	0.52911	0.641145
2069.66437348	1.928	1.46	7167.86	-1.31	900	52.5	0.562065	0.080459	0.103277	0.183022	0.530759	0.69607
2070.70250746	-3.5	1.57	7172.32	-3.47	900	47.8	0.561804	0.078625	0.09964	0.18108	0.529827	0.668034
2071.70780293	-0.88	2.12	7195.44	-4.27	900	39.4	0.589073	0.083154	0.099452	0.180534	0.52584	0.65915
2072.70309705	-2.2	1.86	7185.56	-14.3	900	42.3	0.57986	0.082279	0.098576	0.180502	0.525855	0.654666
2075.63970105	-3.37	1.9	7169.71	0.109	900	45.6	0.594915	0.083487	0.100564	0.181682	0.527055	0.685465
2076.71092255	-6.68	2.31	7174.73	-9.8	900	33.1	0.554061	0.07931	0.103664	0.184892	0.530864	0.665231
2078.68129258	-6.1	1.94	7175.62	-16.9	900	44.2	0.588419	0.082137	0.100369	0.183009	0.534477	0.67444
2079.69077171	-4.53	1.95	7176.88	-8.31	900	45.3	0.560252	0.079819	0.100953	0.183346	0.530948	0.673179
2091.68437135	8.017	1.77	7185.69	-8.84	900	41.1	0.549246	0.082622	0.099392	0.181514	0.526944	0.682402
2092.62561704	-1.48	2.43	7172.71	-7.71	900	34.1	0.581979	0.086567	0.100783	0.183421	0.530712	0.666342
2093.65087003	7.487	7.04	7164.43	-16.6	900	13.4	0.564012	0.107488	0.101191	0.188208	0.50388	0.653611
2094.60798244	-1.1	1.7	7168.72	-6.22	900	42.4	0.5533	0.084541	0.100049	0.184004	0.527844	0.70821
2095.61169299	-0.2	2.3	7152.3	3.952	900	36.4	0.585249	0.077758	0.105133	0.187703	0.525175	0.697218
2096.62962752	-0.29	1.86	7166.3	-11.5	900	46.4	0.541437	0.080363	0.09865	0.182509	0.530522	0.677679
2097.66412402	-2.95	2.64	7180.27	-4.25	900	33.7	0.55499	0.084606	0.102655	0.182256	0.527347	0.650539
2099.63975353	-8.99	2.53	7178.63	-1	900	32.3	0.511441	0.083238	0.09935	0.183486	0.53274	0.664088
2106.65854394	-2.12	2.29	7175.27	-17.8	900	34.3	0.542303	0.089511	0.101622	0.184597	0.529016	0.670419
2110.71566068	-6.18	3.41	7186.25	5.57	900	25.3	0.512902	0.082166	0.101099	0.184164	0.530842	0.67291
2111.55269319	-6.16	1.92	7162.99	-2.12	900	41	0.525014	0.080415	0.100104	0.185605	0.529595	0.68975
2112.58796961	-7.39	1.88	7169.58	-11.6	900	40	0.534984	0.083924	0.099656	0.182888	0.53337	0.680635
2119.69014174	11.98	2.85	7190.32	-9.13	900	25.8	0.545065	0.087481	0.098395	0.182445	0.534123	0.626241
2120.67679558	-2.05	2.87	7208.68	-6.74	900	27.8	0.528515	0.086578	0.102032	0.186926	0.532501	0.627348
2125.54442015	-5.53	3.13	7169.97	-3.52	900	28.1	0.555249	0.085601	0.101368	0.186582	0.523009	0.665638
2126.56835804	-6.72	2.67	7174.3	-16.4	1200	32.1	0.567202	0.083452	0.099046	0.183561	0.527745	0.651399
2127.63415799	0.931	2.18	7180.78	-4.92	900	35.3	0.539365	0.085257	0.098857	0.18364	0.524582	0.655533
2130.59628332	-1.27	3.36	7187.06	-7.56	900	23.7	0.576932	0.083933	0.098713	0.183139	0.531644	0.651165
2134.62011272	0.717	3.58	7200.6	-10.9	900	22.7	0.580358	0.091434	0.100845	0.184286	0.525551	0.661771
2153.55086797	-6.08	1.75	7184.04	-1.32	900	39.9	0.587977	0.087623	0.097656	0.18263	0.528299	0.65772
2153.56077137	-4.39	7.54	7144.15	-24	900	14.5	0.561764	0.077853	0.102889	0.189554	0.527182	0.670189
2156.53992496	-0.87	2.45	7194.74	-1.33	900	34.9	0.596947	0.089431	0.103586	0.187334	0.531839	0.639791
2157.58172574	15.06	6.49	7189.21	8.093	900	15.9	0.554652	0.093102	0.098102	0.18062	0.525648	0.651384
2169.31333487	0.713	5.22	7202.4	-9.03	900	19.2	0.569926	0.086208	0.102926	0.186679	0.532988	0.706365
2170.34375539	-3.22	2.75	7181.57	-5.96	900	26.3	0.573886	0.092071	0.106226	0.189905	0.524569	0.677237
2171.31709456	5.22	2.1	7199.72	-2.35	900	40	0.567555	0.080705	0.097921	0.182549	0.526484	0.643617
2172.31291994	-1.16	1.78	7183.03	-13.1	900	51.7	0.602331	0.082135	0.100467	0.184348	0.521872	0.655749
2189.39389821	-5.12	2.18	7187.35	0.742	900	34.9	0.553612	0.087636	0.106345	0.186232	0.524683	0.636639
2190.35888875	-5.56	2.1	7181.28	-1.38	900	37.8	0.553642	0.08599	0.10436	0.185399	0.52397	0.649955
2192.33613311	-1.58	1.8	7190.22	-4.64	900	41.2	0.594328	0.086471	0.099245	0.182607	0.521139	0.661821
2212.37354384	7.092	3.59	7203.08	-9.36	900	23.9	0.593524	0.09262	0.102766	0.183774	0.521448	0.630614
2213.42063681	16.78	4.42	7211.7	3.168	900	19	0.596428	0.099179	0.101745	0.181668	0.520206	0.654342

Notes. ^(*) Duration of each individual exposure. ^(†) Bisector spans; error bars are twice those of RVs.

Table A.1. continued.

BJD _{UTC} -2457000[days]	RV	$\pm 1\sigma_{RV}$	FWHM	BIS ^(†)	Exp. ^(*)	S/N	$I_{Ca\ ii}$	$I_{H\alpha 06}$	$I_{He\ i}$	$I_{Na\ i}$	$I_{Ca\ i}$	$I_{H\alpha 16}$
–	[m s ⁻¹]	–	–	–	[sec]	–	–	–	–	–	–	–
2216.40383735	-8.94	2.19	7203.82	-10.3	900	33.9	0.594565	0.089359	0.100295	0.182115	0.519823	0.629985
2235.36719701	6.639	2.74	7177.77	0.334	900	25.5	0.595733	0.091527	0.101648	0.182908	0.520753	0.626604
2236.31768047	5.56	2.2	7188.86	-8.92	900	38.7	0.567033	0.087864	0.100285	0.182334	0.518575	0.610068
2237.32364626	4.933	3.21	7181.9	-17.9	1200	28.2	0.559051	0.086238	0.104913	0.186654	0.525845	0.664309
2239.31266431	21.6	2.85	7219.49	1.592	900	31.5	0.591982	0.088633	0.099598	0.180553	0.524177	0.630278
2240.31122271	7.368	2.31	7208.34	-2.51	900	37.6	0.594946	0.081703	0.10278	0.183971	0.522467	0.662409
2244.31706817	6.052	2.84	7195.35	0.352	900	32.5	0.594812	0.084492	0.100398	0.18777	0.524697	0.655945
2245.31980936	0.237	2.24	7209.07	-5.47	900	34.9	0.589965	0.087524	0.103149	0.183372	0.519622	0.663637
2246.32103509	27.1	7.78	7248.46	34.51	1200	12.7	0.594927	0.090211	0.100742	0.184404	0.521228	0.74003
2412.68868670	-3.7	2.54	7163.71	-3.37	900	32.8	0.550281	0.090724	0.100293	0.183955	0.523314	0.6709
2413.66378329	-1.5	2.16	7179.72	-6.74	900	34.4	0.558588	0.088191	0.099293	0.1792	0.526702	0.652927
2414.68886021	2.937	2.15	7166.9	4.331	900	37.1	0.555402	0.084723	0.098655	0.183102	0.530929	0.676626
2416.63114629	2.289	1.95	7191.8	-11.7	900	48	0.584258	0.083699	0.099042	0.180173	0.526418	0.68478
2417.65137234	3.912	1.73	7191.95	-8.14	900	40.8	0.583166	0.087257	0.098779	0.18156	0.52857	0.646774
2418.65486069	4.286	3.33	7195.12	-13.2	900	21.6	0.587824	0.10659	0.10043	0.180994	0.498526	0.662161
2427.73181821	1.618	2.29	7191.43	-0.36	900	34.2	0.595541	0.089463	0.100339	0.183087	0.530979	0.649579
2428.66018094	0.03	3.07	7187.2	-11.9	900	28.1	0.587265	0.089537	0.098802	0.181868	0.526651	0.668995
2430.66988978	-0.96	2.26	7186.32	-3.5	900	36	0.558113	0.085708	0.102817	0.184679	0.529491	0.668576
2431.71360583	-5.64	2.64	7190.54	-22.7	900	32.1	0.550955	0.07889	0.100986	0.181203	0.529026	0.662741
2443.66087057	8.667	3.5	7188.34	-4.35	900	25.2	0.590039	0.092999	0.096614	0.179042	0.526005	0.696153
2444.57982389	9.299	3.32	7180.37	-2.39	900	26.8	0.589859	0.091057	0.098188	0.179557	0.522807	0.666047
2445.59632825	10.81	1.86	7178.02	-8.87	900	36.9	0.557645	0.085087	0.10075	0.181234	0.52886	0.678235
2446.60873425	5.874	1.87	7182.03	2.719	900	45	0.552972	0.085681	0.101935	0.183638	0.525628	0.682197
2447.61736597	1.855	2.1	7181.21	-2	900	39.9	0.585974	0.086557	0.101268	0.182021	0.529423	0.6903
2448.59166621	2.524	1.79	7183.26	-6.53	900	46.5	0.550409	0.081722	0.099201	0.181717	0.528627	0.676518
2449.61666267	-2.34	1.85	7181.85	-9.02	900	46.7	0.55726	0.081361	0.100242	0.183494	0.527072	0.693437
2453.58138876	-5.57	2.17	7179.71	-10.5	900	38.1	0.576	0.087524	0.101564	0.182982	0.529699	0.666481
2454.66732062	-2.11	5	7157.53	-13.6	900	16.4	0.534792	0.105417	0.106316	0.186865	0.531533	0.672621
2455.68136136	1.242	2.34	7201.87	-15	900	37.6	0.559782	0.085698	0.097922	0.182038	0.527513	0.642527
2456.70358427	1.194	1.71	7193.3	-2.59	900	39.1	0.539261	0.083335	0.100678	0.18192	0.526882	0.654302
2457.65444875	0.232	1.53	7186.93	-4.04	900	45.9	0.544456	0.082158	0.103781	0.185289	0.52979	0.678245
2458.62416725	1.797	2.1	7191.62	-2.73	900	42.5	0.571849	0.083688	0.10082	0.181891	0.525159	0.670374
2459.58868774	0	2.42	7166.31	-9.47	900	32	0.534143	0.084143	0.101018	0.183983	0.531303	0.671843
2460.68008744	2.859	2	7199.43	-10	900	39	0.567005	0.085291	0.09952	0.182178	0.53004	0.641539
2461.61247483	-3.43	2.01	7177.71	-14.6	900	39.8	0.531283	0.081882	0.101482	0.18371	0.532312	0.662684
2462.59699290	-1.49	2.41	7193.46	-10.2	900	34	0.53251	0.091757	0.1007	0.182059	0.53047	0.678952
2464.59087617	5.604	5.45	7198.52	-24.4	900	17.8	0.536789	0.095036	0.099161	0.183787	0.528055	0.686225
2465.55285533	1.953	1.95	7189.61	-10.6	900	37.5	0.525385	0.081987	0.102391	0.184078	0.528833	0.659363
2472.64437339	9.088	3.09	7206.96	-15.6	900	28.8	0.582423	0.088182	0.102267	0.18471	0.526636	0.671635
2473.58211801	-2.46	3.71	7182.04	-22.5	900	24	0.548713	0.090743	0.100974	0.184532	0.522132	0.670676
2475.57083577	3.505	2.35	7184.54	-16.3	1800	32.2	0.580897	0.092011	0.101234	0.182594	0.528772	0.656172
2476.56282582	7.827	1.91	7191.68	-6.25	900	44	0.556952	0.083328	0.09885	0.181388	0.523729	0.660628
2477.54247641	5.777	1.95	7190.45	-13.2	900	40.1	0.584375	0.084401	0.105974	0.186686	0.528026	0.684554
2478.53938306	3.887	2.42	7199.21	1.209	900	33.4	0.542519	0.091376	0.099644	0.180595	0.522094	0.662569
2479.53060547	0.796	2.4	7200.54	-6.9	900	35.5	0.578876	0.086324	0.099936	0.181075	0.527574	0.654195
2481.49382164	3.548	2.82	7186.71	-6.58	900	31.2	0.53899	0.091801	0.101227	0.183502	0.527366	0.676158
2513.44982261	1.106	2.07	7176.01	-3.44	900	41.6	0.561363	0.088328	0.100405	0.183709	0.523996	0.678603
2513.50218232	-4.57	2.69	7172.76	-4.86	900	33.2	0.566953	0.08974	0.10596	0.188059	0.524511	0.666513
2515.41917706	-2.34	1.93	7184.92	-5.97	900	41.7	0.564153	0.089897	0.101247	0.182411	0.526736	0.673459
2515.44453511	-3.02	1.76	7178.72	-6.73	900	49.2	0.567076	0.088259	0.098628	0.181831	0.520853	0.679953
2516.53077561	-4.93	2.92	7190.8	1.972	900	31.9	0.602149	0.092247	0.099896	0.182444	0.527717	0.666103
2565.36649887	0.845	1.64	7187.23	-3.3	900	54.5	0.596593	0.088658	0.09841	0.180042	0.522949	0.675468
2566.34542939	-5.47	2.15	7179.09	-6.14	900	45.4	0.601739	0.091592	0.099575	0.18055	0.525212	0.678527
2575.40497038	3.93	2.12	7181.99	-8.36	900	40.1	0.566264	0.087701	0.098051	0.182169	0.523518	0.671318
2579.38524573	5.059	2.18	7191.98	-5.62	900	38.3	0.562049	0.089366	0.104764	0.183719	0.523329	0.674917
2580.41266409	10.09	5.97	7187.22	4.876	900	19.9	0.572011	0.107006	0.107628	0.185394	0.52275	0.687077
2584.33980519	0.821	2.95	7183.34	0.433	900	29.2	0.56581	0.092026	0.104575	0.185035	0.514433	0.687819
2588.34483394	1.991	5.05	7181.58	9.001	900	19.2	0.560173	0.094073	0.110324	0.186892	0.524911	0.680451
2601.31675212	5.918	2.03	7196.44	-6.76	900	45.2	0.565656	0.087291	0.10094	0.17769	0.523886	0.667702

Notes. ^(*) Duration of each individual exposure. ^(†) Bisector spans; error bars are twice those of RVs.

Appendix B: Priors and posteriors

Table B.1. Prior volume for the parameters of the one-planet model fit of Sect. 2.3 processed with `juliet`. $\mathcal{U}(a, b)$ indicates a uniform distribution between a and b ; $\mathcal{L}(a, b)$ a log-normal distribution, $\mathcal{N}(a, b)$ a normal distribution, and $\mathcal{T}(a, b)$ a truncated normal distribution (where lower possible value equals zero) with mean a and standard deviation b .

Parameter	Prior distribution
Keplerian Parameters:	
ρ_\star [kg/m ³]	$\mathcal{N}(1300, 100)$
$T_{0,b}$ [BJD]	$\mathcal{N}(2458745.921, 0.003)$
P_b [days]	$\mathcal{N}(12.998, 0.002)$
e_b^*	0
ω_b^*	90
Transit Parameters:	
R_p/R_\star	$\mathcal{U}(0.0, 1.0)$
D	1.0
q_1	$\mathcal{N}(0.31, 0.30)$
q_2	$\mathcal{N}(0.25, 0.10)$
Light curve GP Hyperparameters:	
σ_{TESS} [ppt]	$\mathcal{L}(10^{-3}, 10)$
ρ_{TESS} [days]	$\mathcal{L}(10^{-1}, 10)$
RV parameters:	
K_b [m/s]	$\mathcal{U}(0.0, 10.0)$
$\sigma_{\text{HARPS-N}}$ [m s ⁻¹]	$\mathcal{U}(0, 10)$
A [m s ⁻¹ days ⁻¹]	$\mathcal{U}(-1, 1)$
B [m s ⁻¹]	$\mathcal{U}(-20, 20)$

Notes. ^(*) In the case of non-null eccentricity, the priors were set as follows: ($\sqrt{e} \sin \omega$, $\sqrt{e} \cos \omega$) in $\mathcal{U}(-1.0, 1.0)$.

Table B.2. Prior volume for the parameters of the two-planet model fit of Sect. 2.3 processed with `juliet`.

Parameter	Prior distribution
Keplerian Parameters:	
ρ_\star [kg/m ³]	$\mathcal{N}(1300, 100)$
$T_{0,b}$ [BJD]	$\mathcal{N}(2458745.921, 0.003)$
P_b [days]	$\mathcal{N}(12.998, 0.002)$
$T_{0,c}$ [BJD]	$\mathcal{N}(2458740, 2458790)$
P_c [days]	$\mathcal{U}(1, 100)$
$(e_b, e_c)^*$	0
$(\omega_b, \omega_c)^*$	90
Transit Parameters:	
R_p/R_\star	$\mathcal{U}(0.0, 1.0)$
D	1.0
q_1	$\mathcal{N}(0.31, 0.30)$
q_2	$\mathcal{N}(0.25, 0.10)$
Light curve GP Hyperparameters:	
σ_{TESS} [ppt]	$\mathcal{L}(10^{-3}, 10)$
ρ_{TESS} [days]	$\mathcal{L}(10^{-1}, 10)$
RV parameters:	
K_b [m/s]	$\mathcal{U}(0.0, 10.0)$
K_c [m/s]	$\mathcal{U}(0, 10)$
$\sigma_{\text{HARPS-N}}$ [m s ⁻¹]	$\mathcal{U}(0, 10)$
A [m s ⁻¹ days ⁻¹]	$\mathcal{U}(-1, 1)$
B [m s ⁻¹]	$\mathcal{U}(-20, 20)$

Notes. ^(*) In the case of non-null eccentricity, the priors were set as follows: ($\sqrt{e} \sin \omega$, $\sqrt{e} \cos \omega$) in $\mathcal{U}(-1.0, 1.0)$.

Table B.3. Posterior's result for the parameters of the two-planet eccentric model fit of Sect. 2.3 processed with `juliet`.

Parameter	Value ($\pm 1\sigma$)
Keplerian Parameters:	
ρ_\star [kg/m ³]	1312^{+55}_{-68}
a_b/R_\star	$22.72^{+0.31}_{-0.40}$
a_c/R_\star	$39.05^{+0.50}_{-0.73}$
$T_{0,b}$ [BJD]	$2458745.9205^{+0.0012}_{-0.0011}$
P_b [days]	12.9972 ± 0.0006
$T_{0,c}$ [BJD]	$2458776.6^{+4.5}_{-4.6}$
P_c [days]	$29.29^{+0.21}_{-0.20}$
Transit Parameters:	
R_{pb}/R_\star	$0.0356 \pm^{+0.0007}_{-0.0005}$
q_1	$0.28^{+0.11}_{-0.08}$
q_2	$0.30^{+0.05}_{-0.05}$
b_b	$0.19^{+0.11}_{-0.10}$
i_b [deg]	$89.52^{+0.26}_{-0.28}$
Light curve GP Hyperparameters:	
σ_{TESS} [ppt]	$0.19^{+0.03}_{-0.02}$
ρ_{TESS} [days]	$0.76^{+0.19}_{-0.15}$
RV parameters:	
K_b [m/s]	$2.47^{+0.50}_{-0.46}$
K_c [m/s]	$2.36^{+0.42}_{-0.40}$
$\sigma_{\text{HARPS-N}}$ [m s ⁻¹]	$2.93^{+0.35}_{-0.32}$
A [m s ⁻¹ days ⁻¹]	0.0110 ± 0.0015
B [m s ⁻¹]	-9.1 ± 1.3

Appendix C: Corner plots

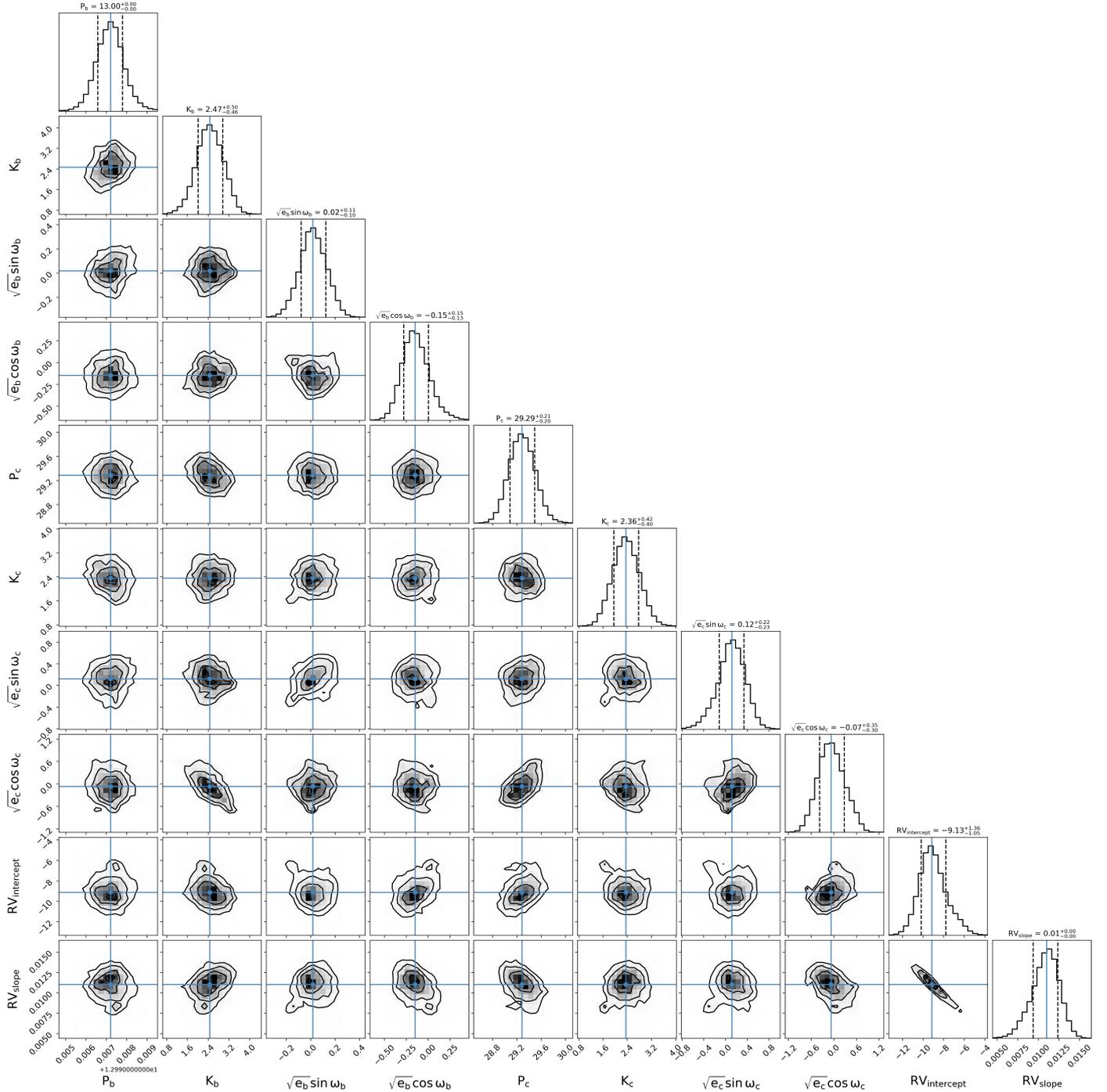


Fig. C.1. Corner plot for the posterior distribution of the joint transit and RV analysis of Sect. 3.3 in the case of two planets, elaborated with juliet.

Appendix D: Additional plots

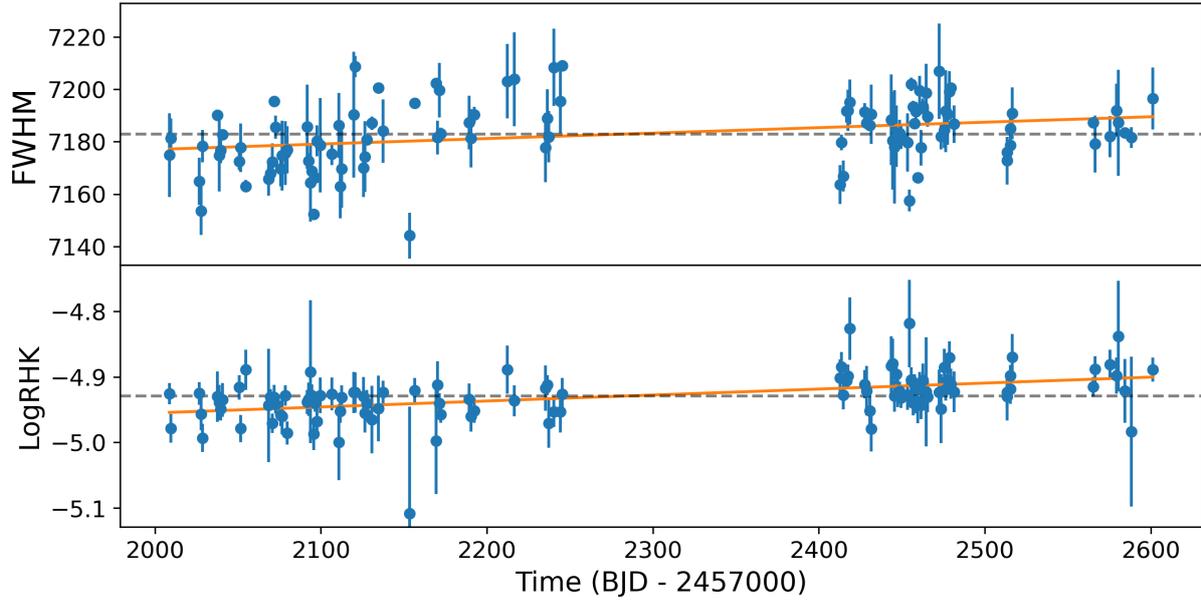


Fig. D.1. FWHM and $\log R'_{\text{HK}}$ are plotted over time respectively in the upper and lower panel, along with their linear trends (orange line) and average value (dashed grey line).

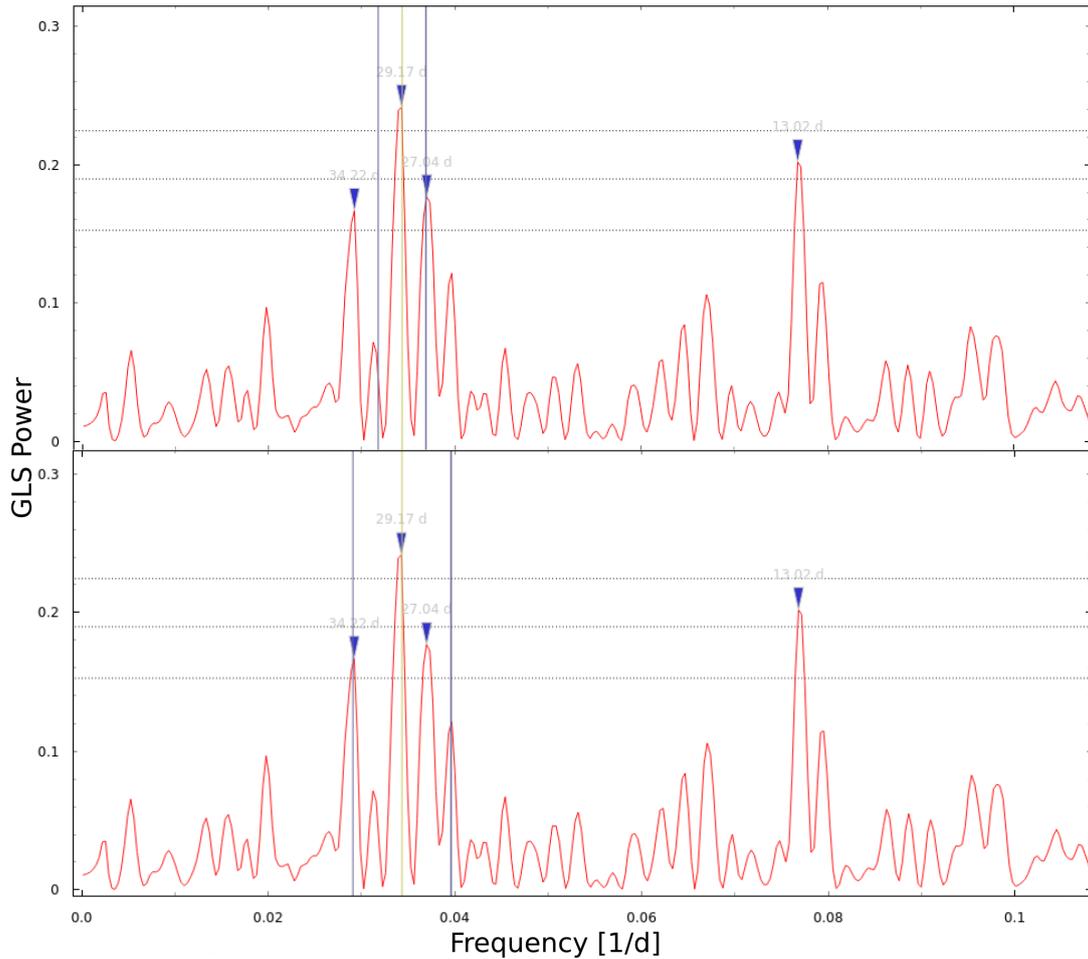


Fig. D.2. Close-up look of the RV GLS periodogram, executed with the publicly available tool Exo-Striker (Trifonov 2019; <https://github.com/3fon3fonov/exostriker>) after the removal of a linear trend. The two vertical blue lines, around the 29-day signal (indicated by a vertical yellow line), show the main peak aliases due to the two highest frequencies of the window function, in the upper and bottom panels. The three horizontal dotted lines represent the 10%, 1%, and 0.1% FAP levels.

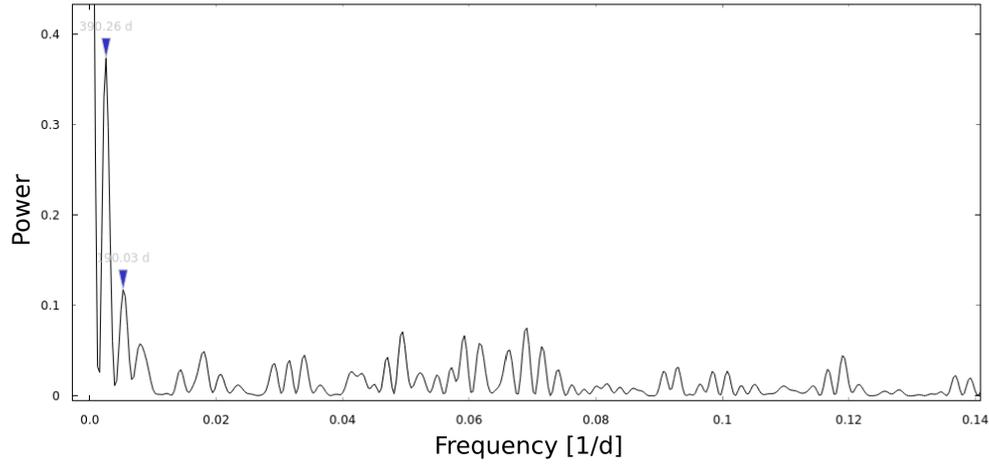


Fig. D.3. Window function of the HARPS-N RV measurements, as evaluated with Exo-Striker. The two highest peaks, excluding the 1-day peak and frequencies close to zero, are indicated by the respective labels.

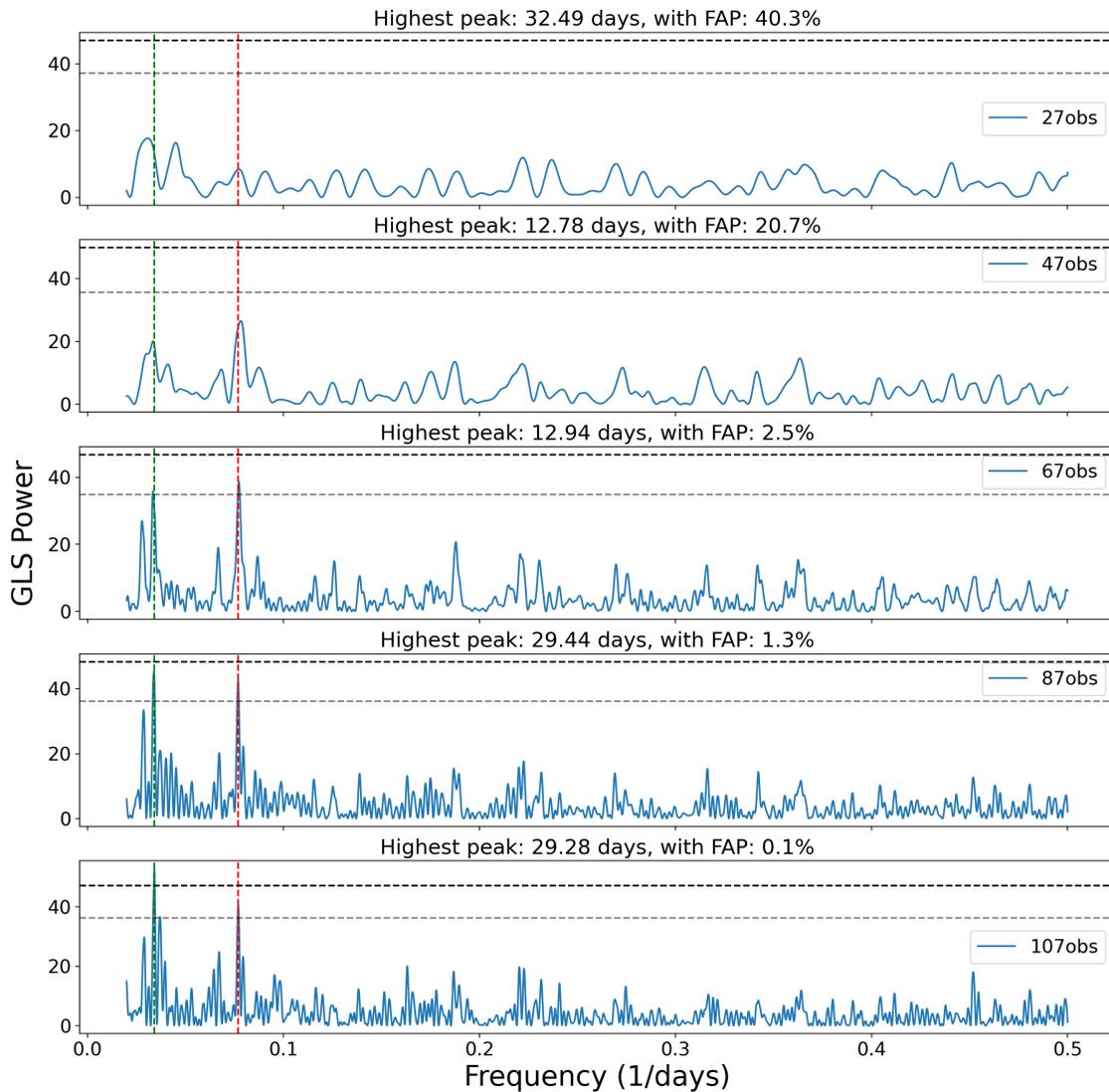


Fig. D.4. Unnormalized GLS power for a different number of HARPS-N observations. The power of the 29-day signal increases with more observations. The vertical dashed red and green lines indicate TOI-1422 b and TOI-1422 c orbital periods, respectively, while the horizontal dashed lines signal the 10% and 1% confidence levels, respectively (evaluated with the bootstrap method).

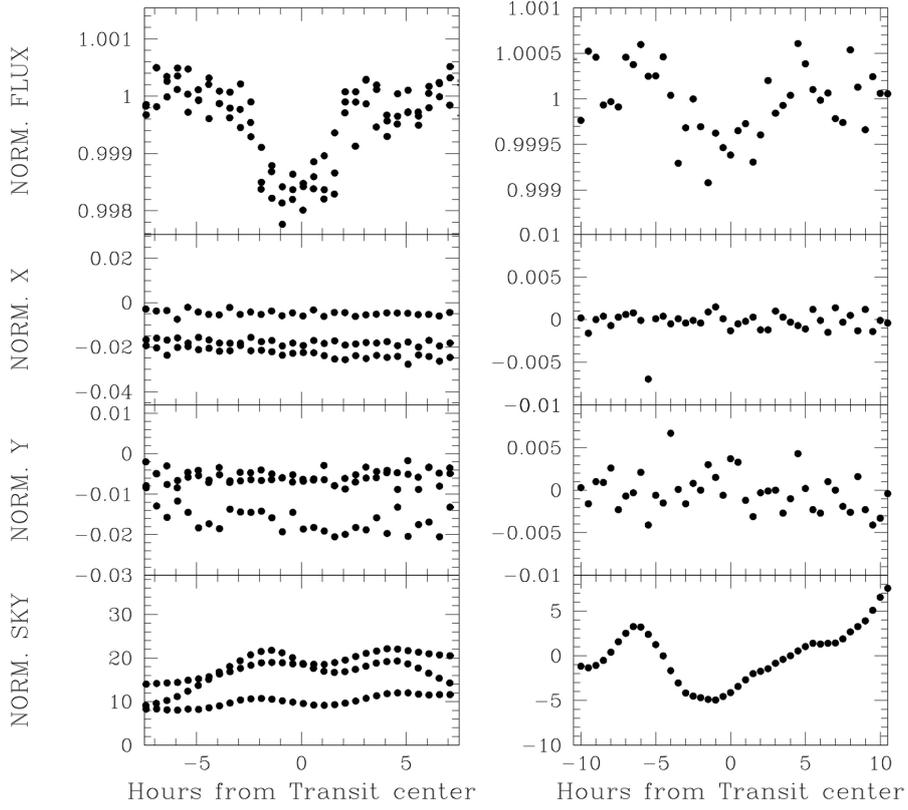


Fig. D.5. TOI-1422 b transits, as seen with PATHOS, folded on the first row of the left column and the single transit event on the right one, with X/Y and the sky background in the following rows, showing no correlation with the transits.

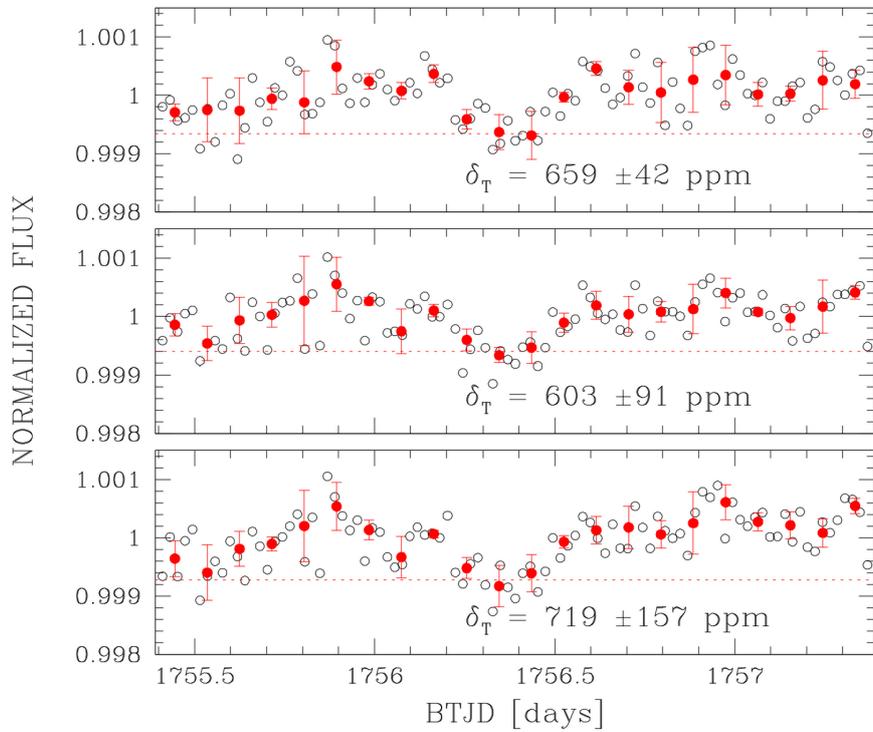


Fig. D.6. Single transit depth from PATHOS in different apertures, with the three rows showing the transit depth at an aperture radius of 2, 3, and 4 pixels, respectively.